



Phénomènes de relaxation dans les verres

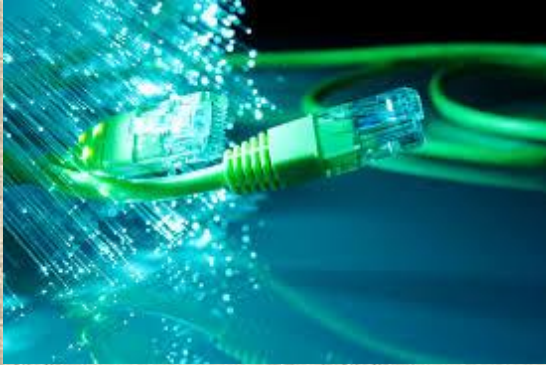
Yann Vaills

Orléans University

***Conditions Extrêmes des Matériaux : Haute
Température et Irradiation***

CEMHTI UPR 3079 CNRS

Ageing of glasses...?



Nuclear waste



household refuse

Ageing of glasses

Chemical reasons

physical reasons

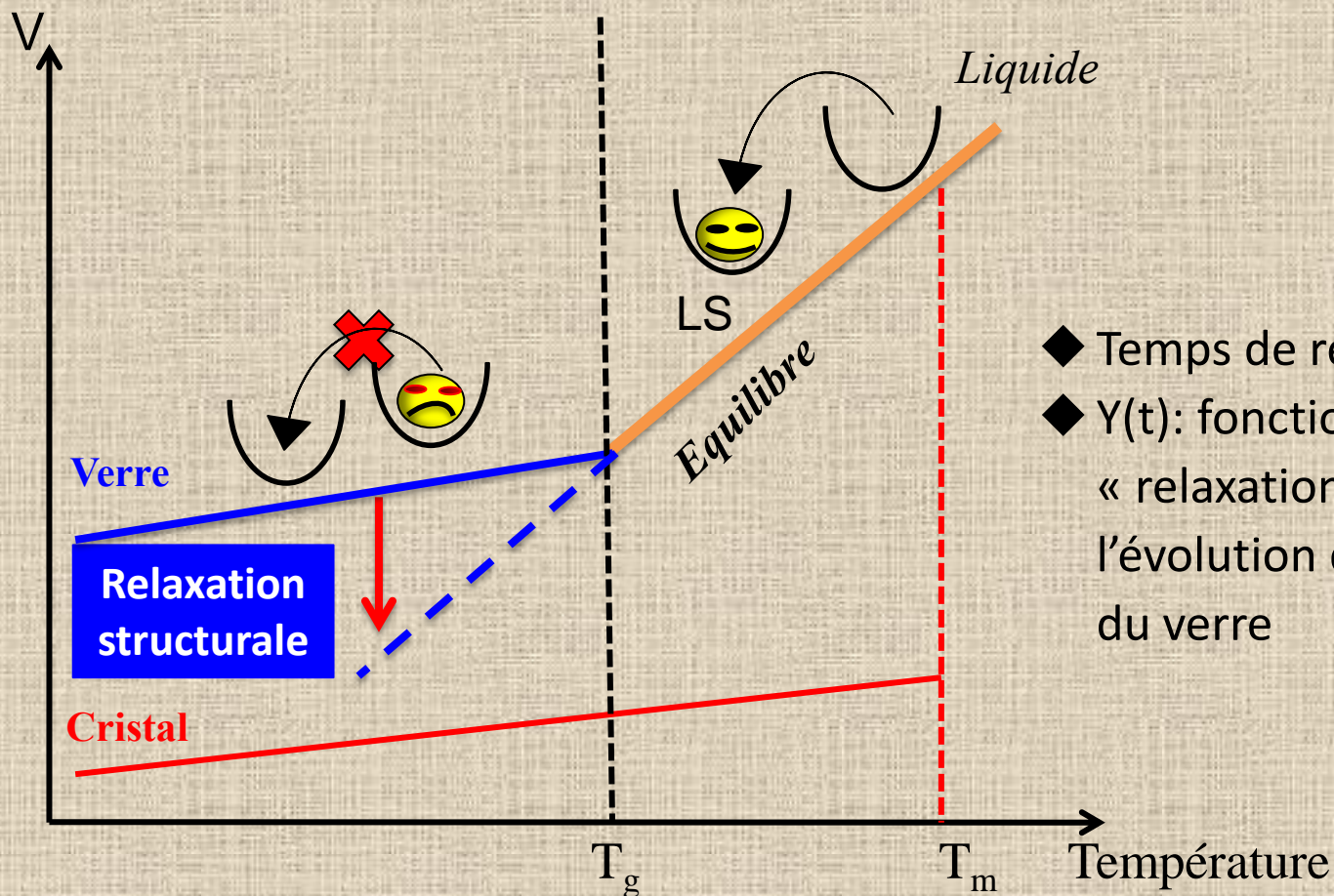
Le verre obtenu par refroidissement d'un liquide surfondu



Systeme hors-équilibre

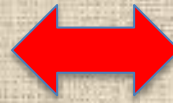
$T, P, t \dots$

Equilibre



- ◆ Temps de relaxation τ
- ◆ $Y(t)$: fonction dite de « relaxation » qui traduit l'évolution d'une propriété du verre

Outil de mesure
temps expérience T_{exp}



Fonction de
relaxation $y(t)$

sollicitation en température : expérience en temps

T



temps

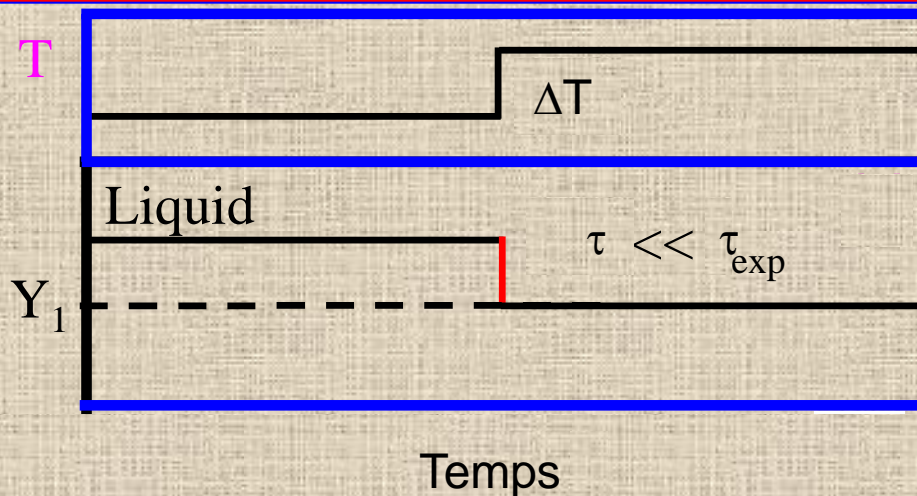
Outil de mesure
 temps expérience T_{exp}



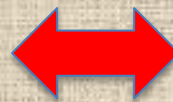
Fonction de relaxation $y(t)$

sollicitation en température : expérience en temps

à l'état liquide



Outil de mesure
 temps expérience T_{exp}



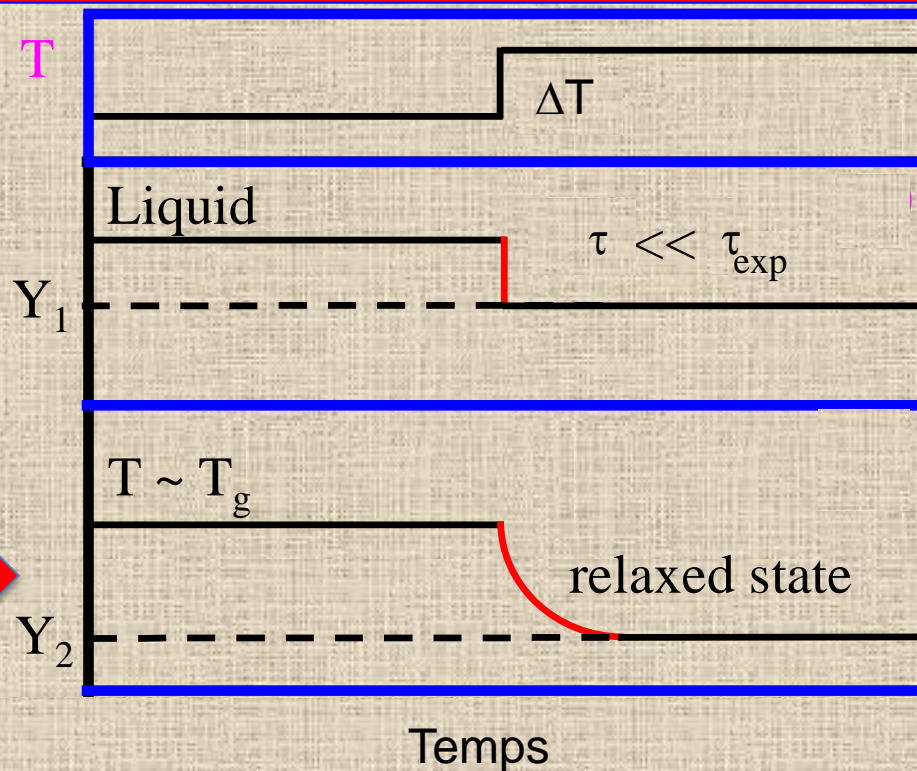
Fonction de relaxation $y(t)$

sollicitation en température : expérience en temps

à l'état liquide



dans l'intervalle de T_g



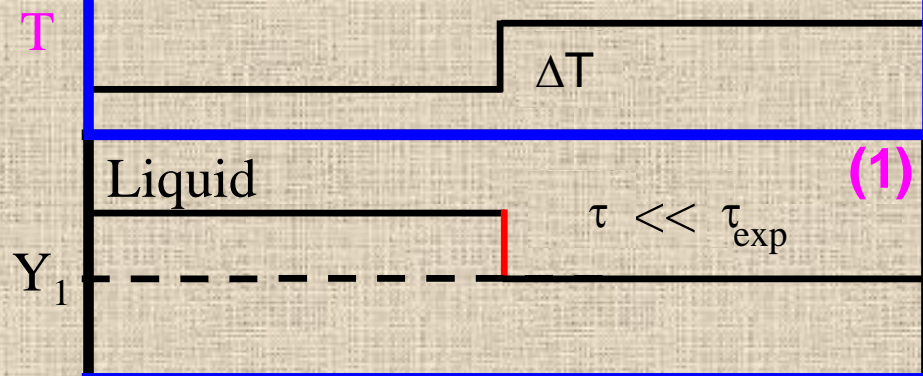
Outil de mesure
 temps expérience T_{exp}



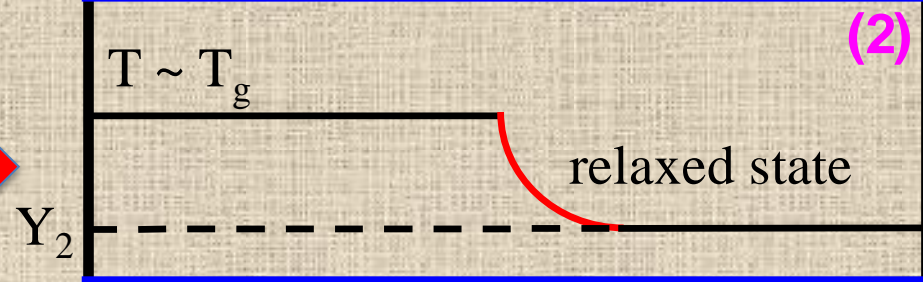
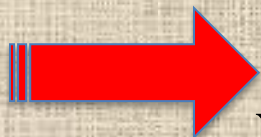
Fonction de relaxation $y(t)$

sollicitation en température : expérience en temps

à l'état liquide



dans l'intervalle de T_g



à la température ambiante



Time

Heterogeneous dynamics relaxation

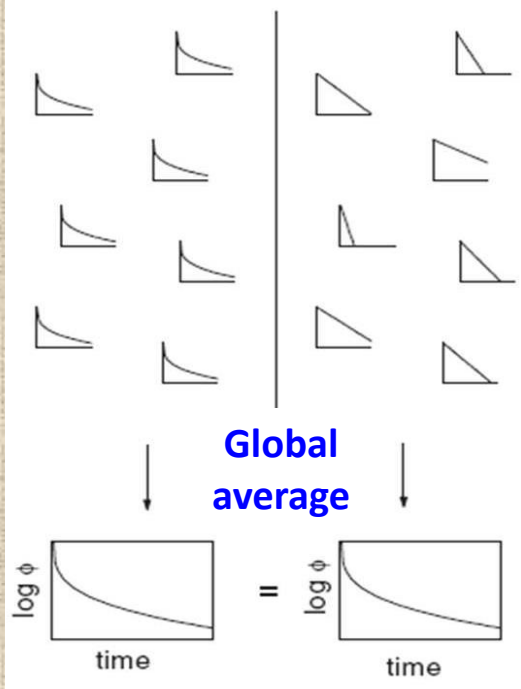
Polymers, molecular glasses...

$Y(t) \rightarrow$ several relaxation processes

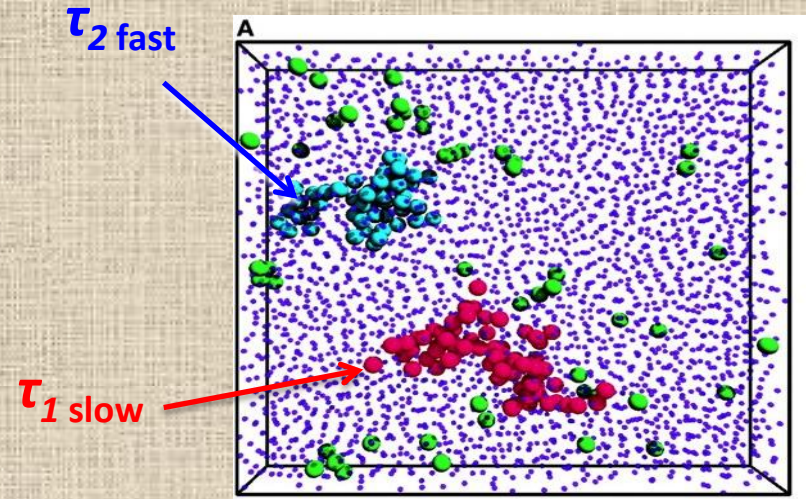
$$y(t) = \sum_{i=1}^n y_{0i} \exp\left(\frac{-t}{\tau_i}\right)$$

Homogeneous dynamics

Heterogeneous dynamics



Colloidal solution $T < T_g$



E.R. Weeks, Science (2000)

$$y(t) = y_0 - w \exp\left(\frac{-t}{\tau}\right)^\beta$$

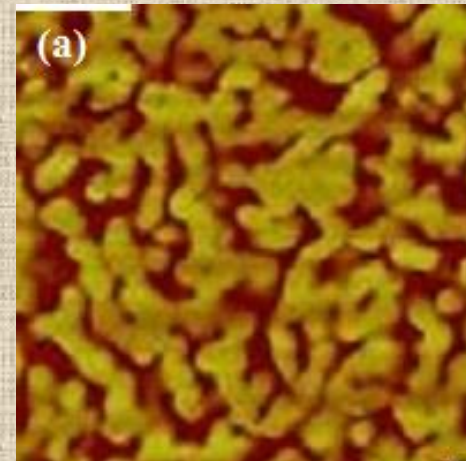
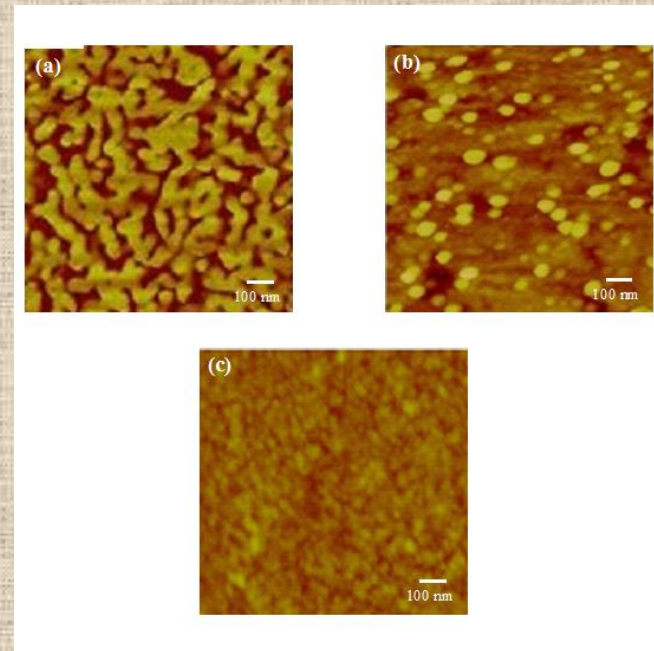
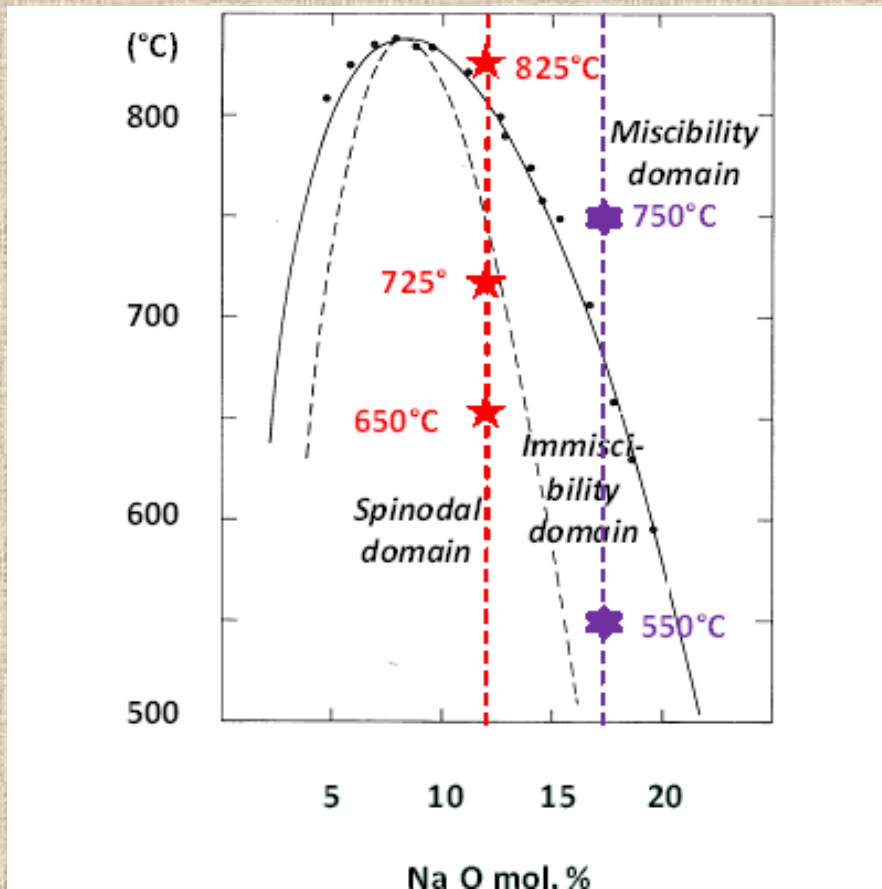
What about oxide glasses?

\rightarrow Oxide glasses : chemical and topological heterogeneity

\rightarrow Dynamics and nature of relaxation are depending on the spatial scale

Composition choose

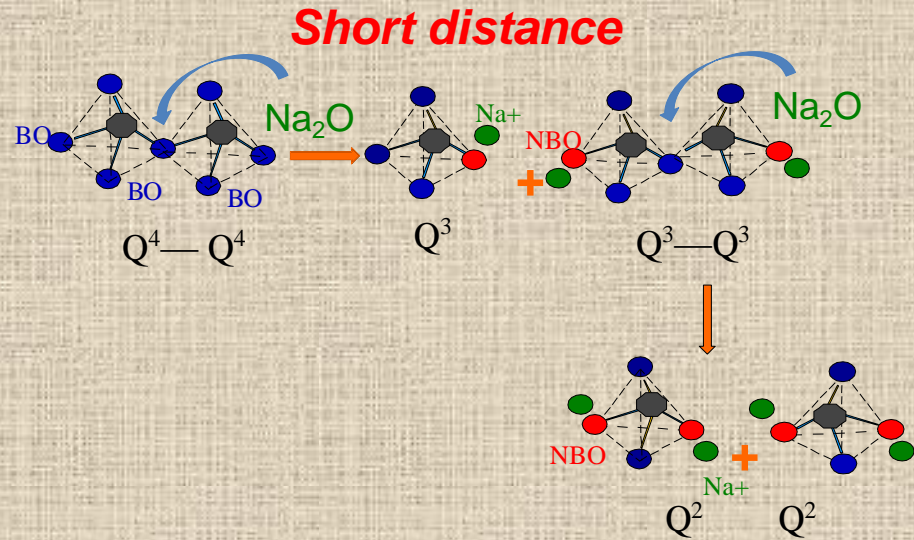
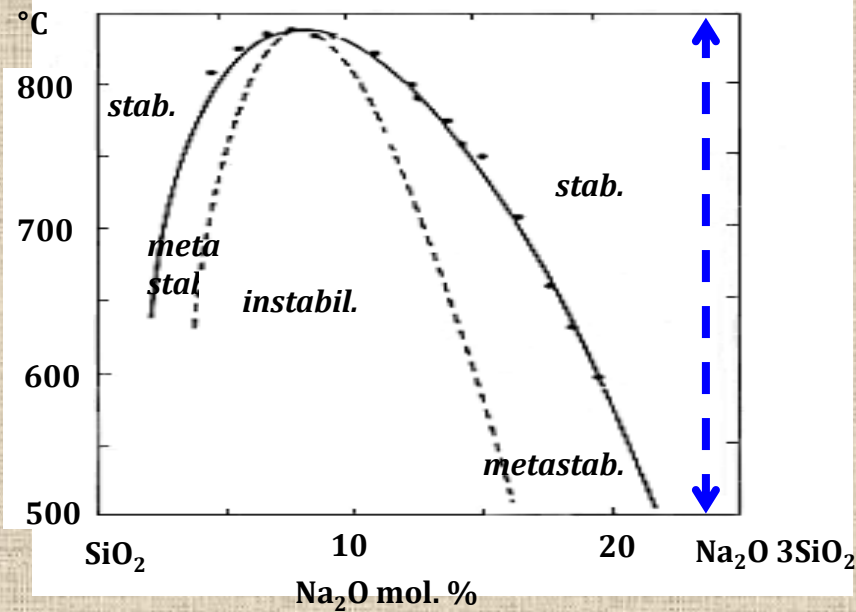
Composition $x\text{Na}_2\text{O} - (1-x)\text{SiO}_2$



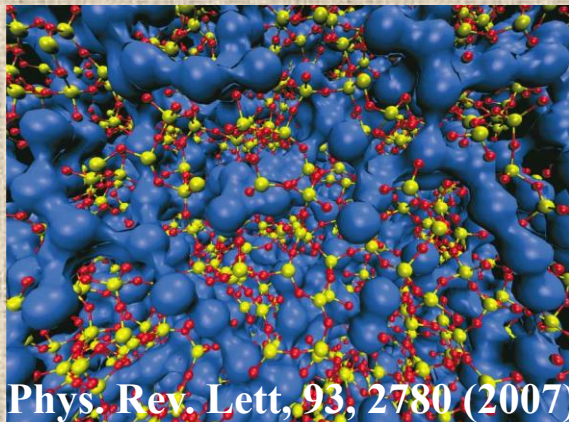
Composition choose

Composition 0.27 Na₂O- 0.73 SiO₂

✓ T_g(DSC) = 730K

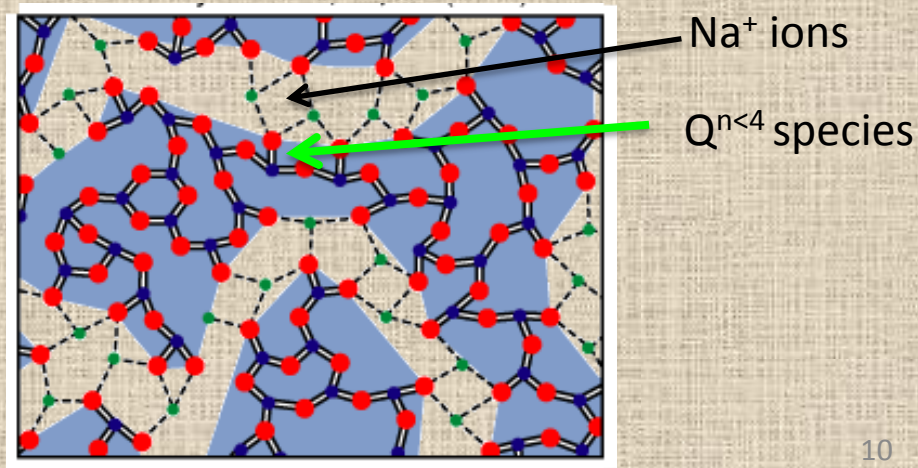


Long distance
Modified random model
Greaves, JNCS (1985)



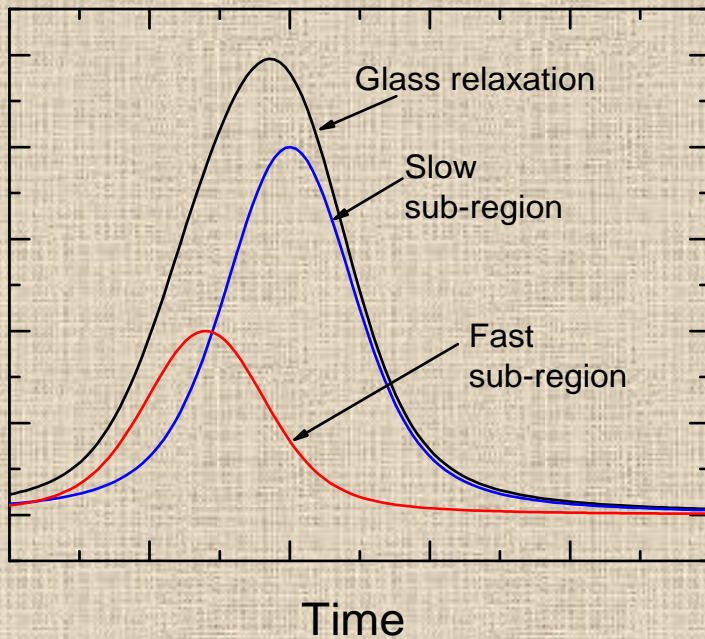
*Neutron scattering
 + Molecular Dynamics
 calculations*

Phys. Rev. Lett, 93, 2780 (2007)



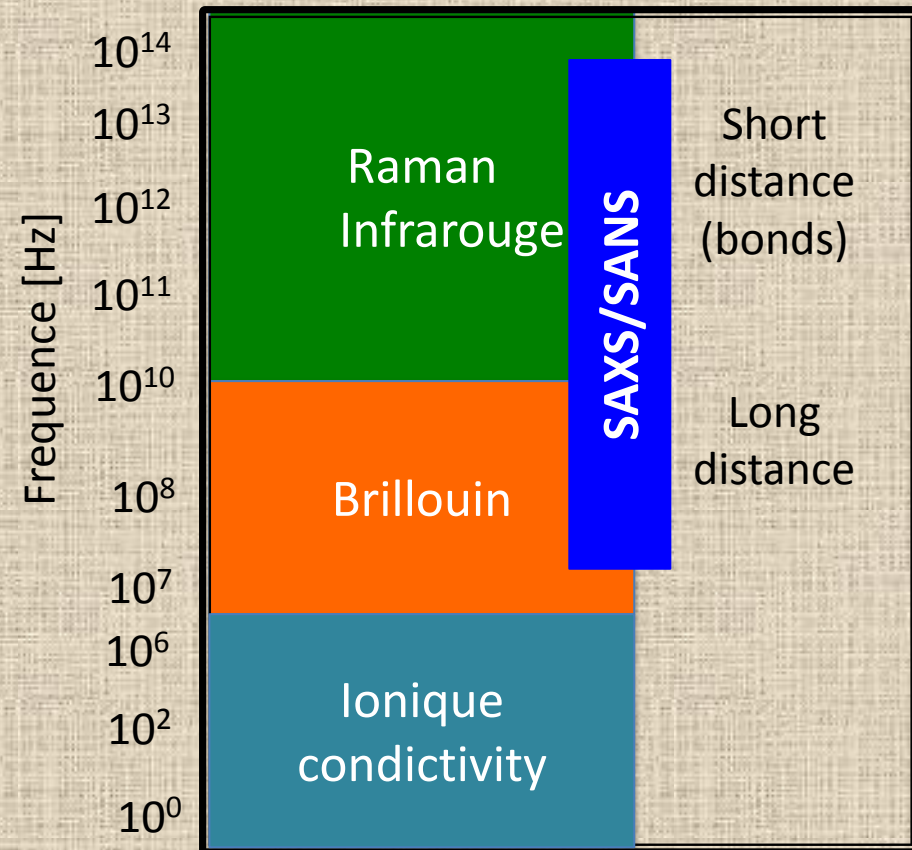
Wich scale?

Idea



R. Ritchert, J. Phys. Cond. Mat. (2002)

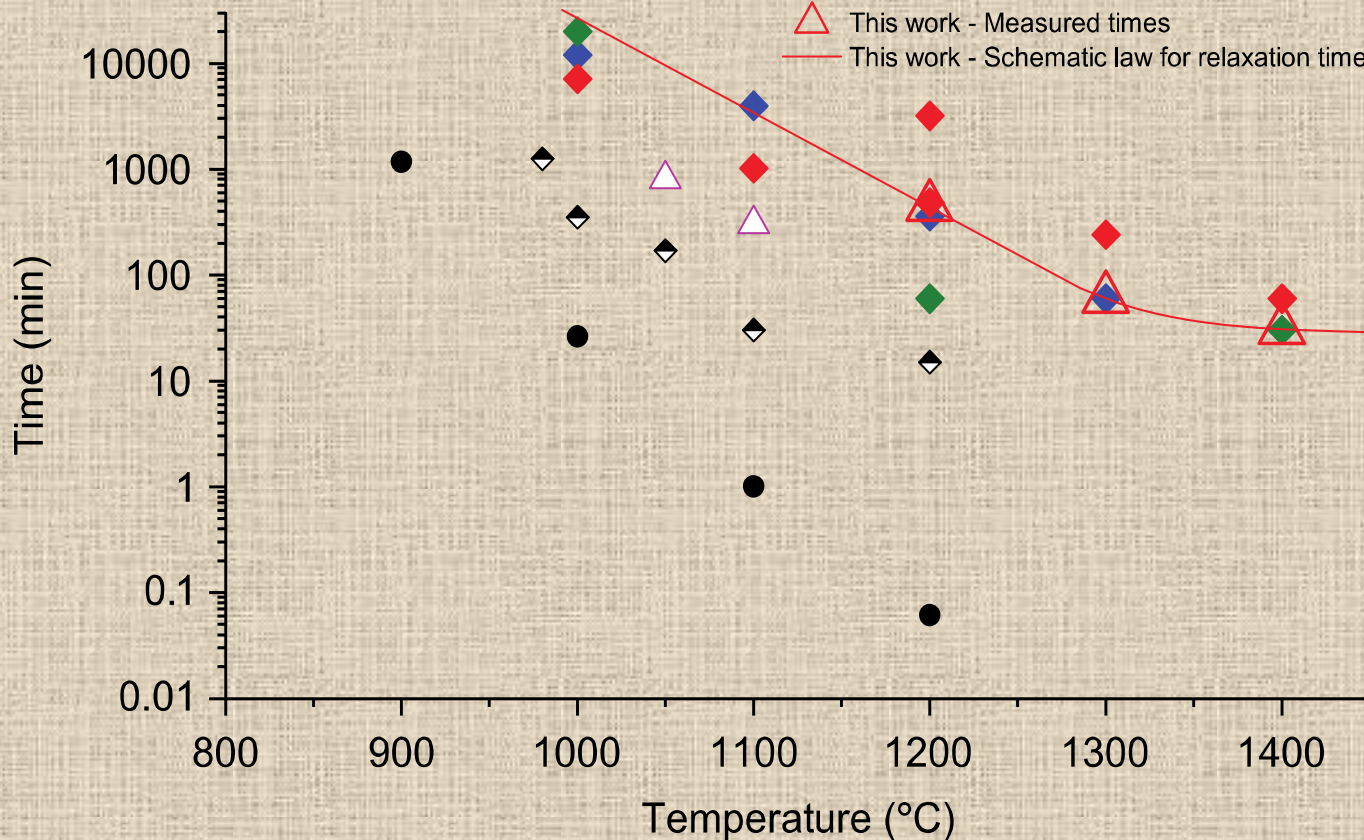
tools



Structural relaxation

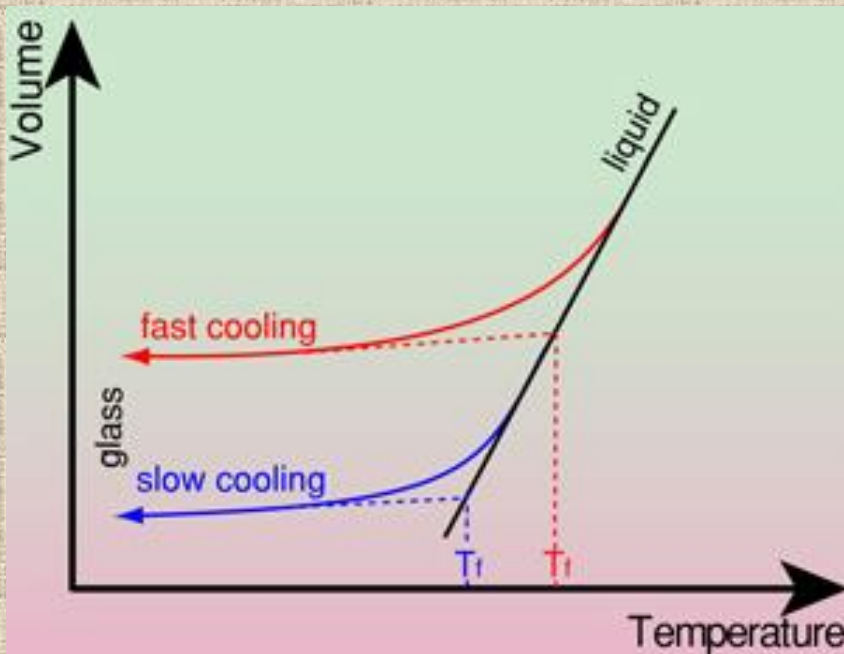
Relaxation function $y(t,T)$

- circles : calculated times*
 - Dingwell 1990 - Relaxation times deduced from viscosity
- diamonds : annealing times*
 - ◆ Ryu 2006 - Annealing times (IR)
 - ◊ Goller 2009 - Annealing times (Raman)
 - ◆ Bibent 2009 - Annealing times (IR)
 - ◆ This work - Annealing times
- triangles : measured times*
 - △ Tomozawa 2008 - Measured times after RT quenching (IR)
 - △ This work - Measured times
- This work - Schematic law for relaxation times

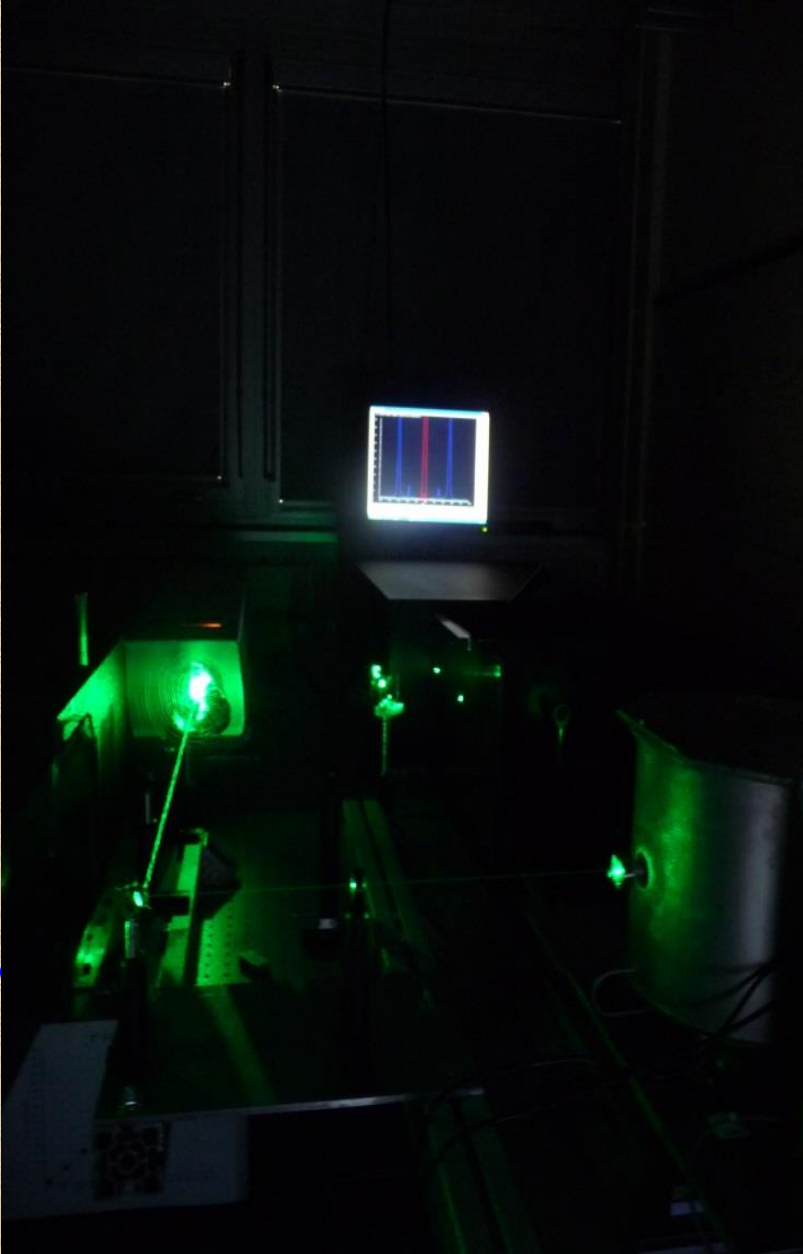


Structural relaxation

Which relaxation function $y(t)$?



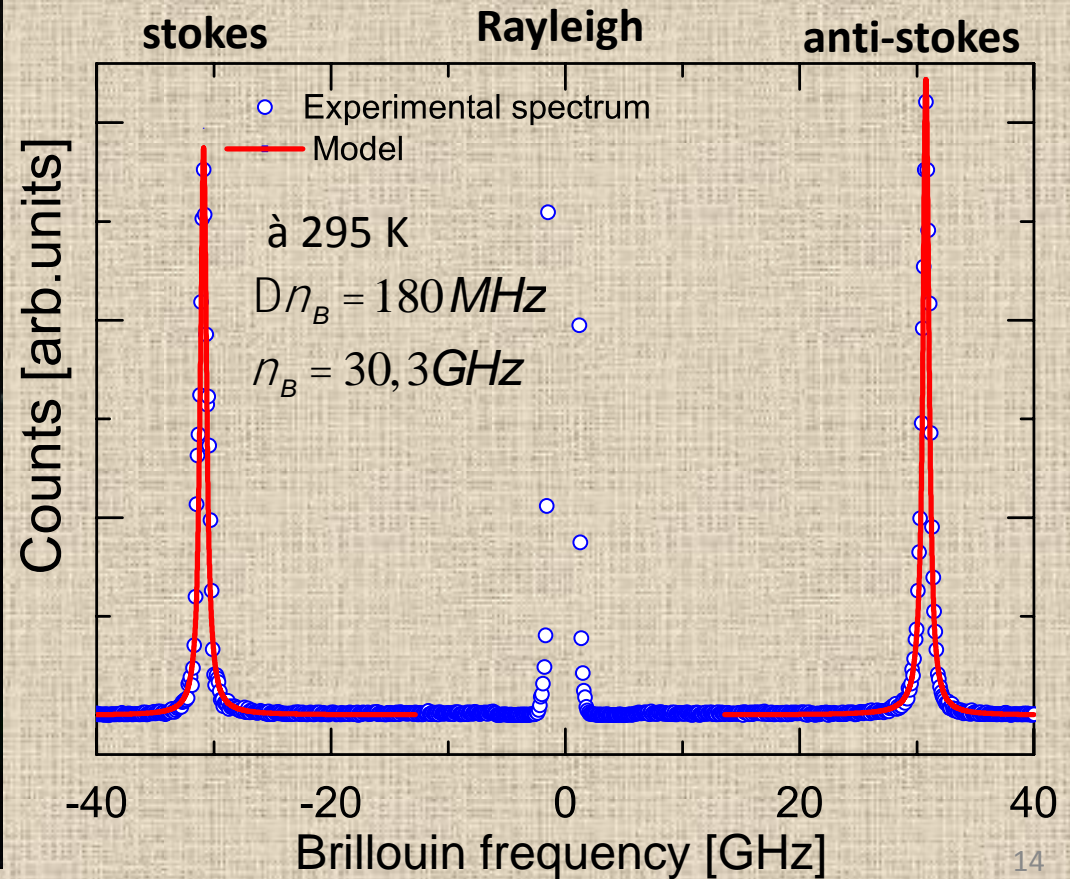
- ✓ Longitudinal acoustical mode frequency (measured by Brillouin scattering)
- ✓ Relative intensity of an Raman lines



s)

$$I = I_{Dho} \ddot{A} I_{instr}$$

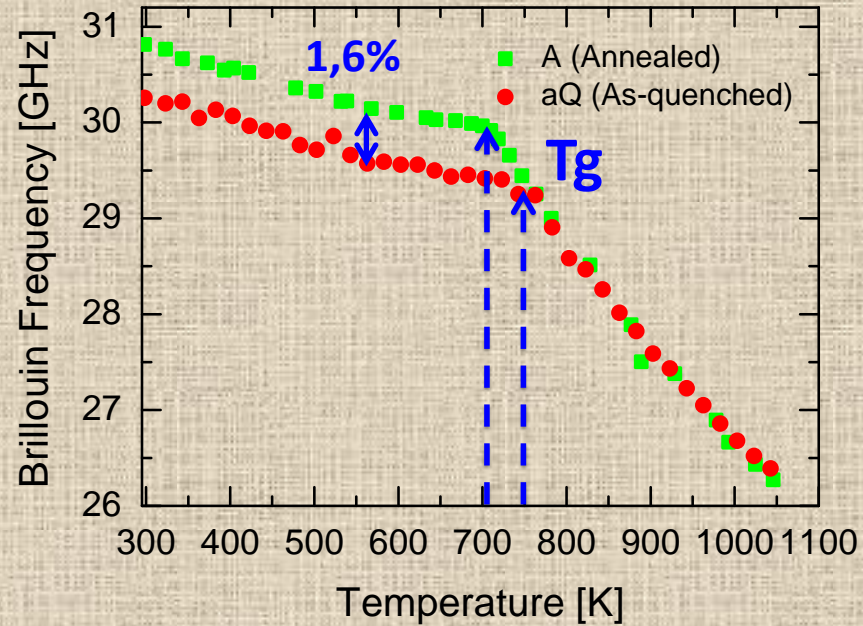
$$I_{Dho} = \frac{I}{4\rho} \frac{4Dn_B n_0^2}{(n^2 - n_0^2) + 4n^2 Dn_B}$$



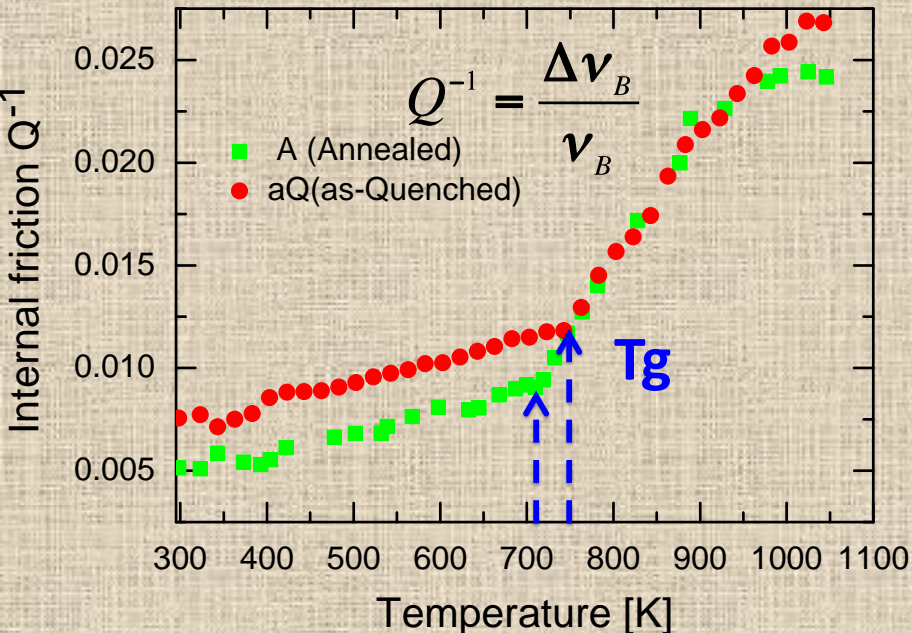
Brillouin scattering vs Temperature

Brillouin frequency variations

- *As quenched glass*
- *Annealed glass*



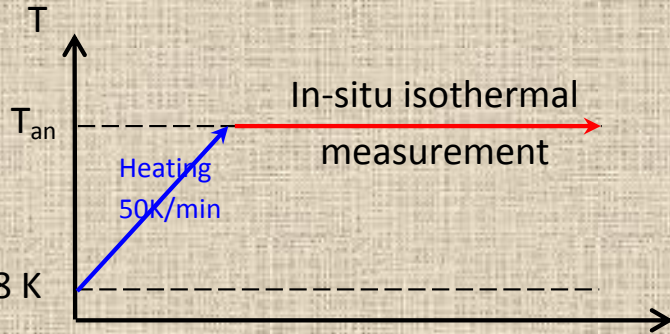
Internal friction variations



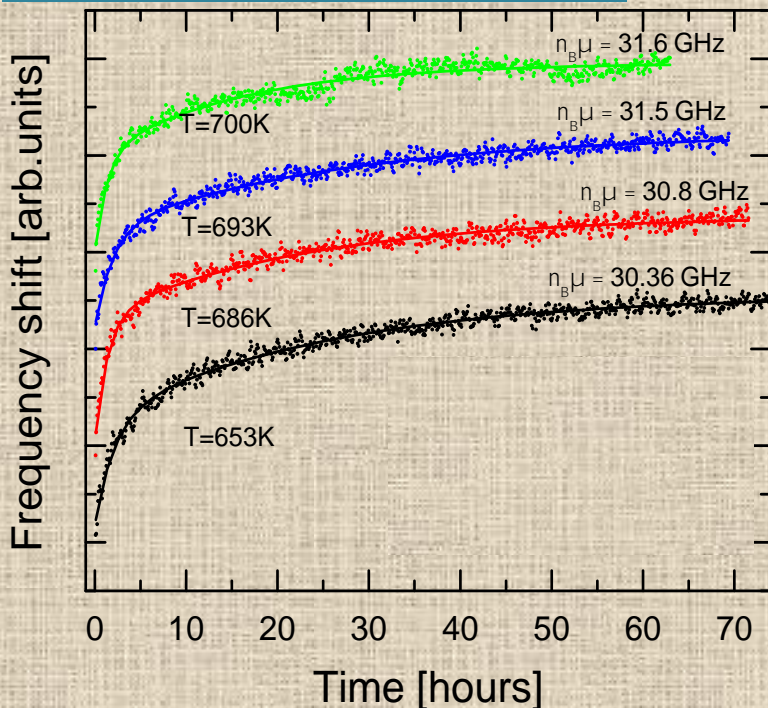
→ Two signatures of a long distance relaxation

Brillouin scattering vs Temperature & time

Experimental procedure for relaxation study

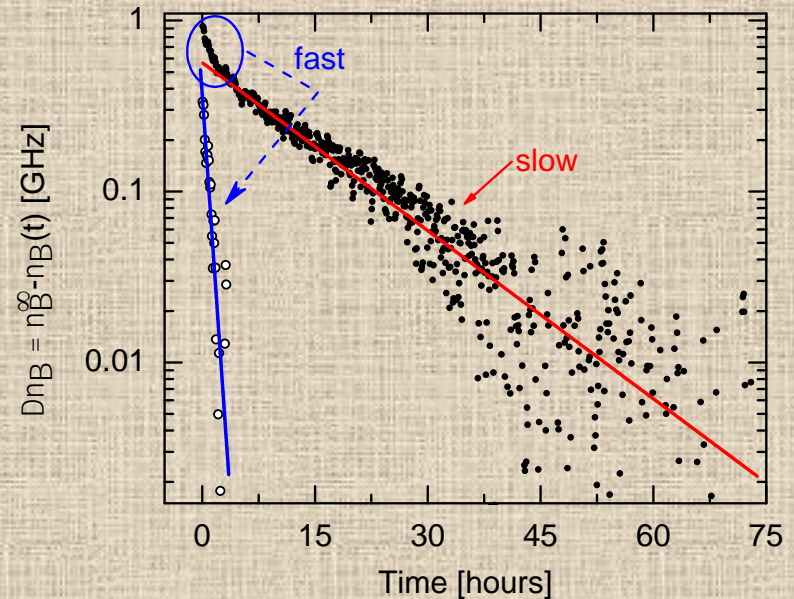


Relaxation kinetics



analyse

Exponential decomposition



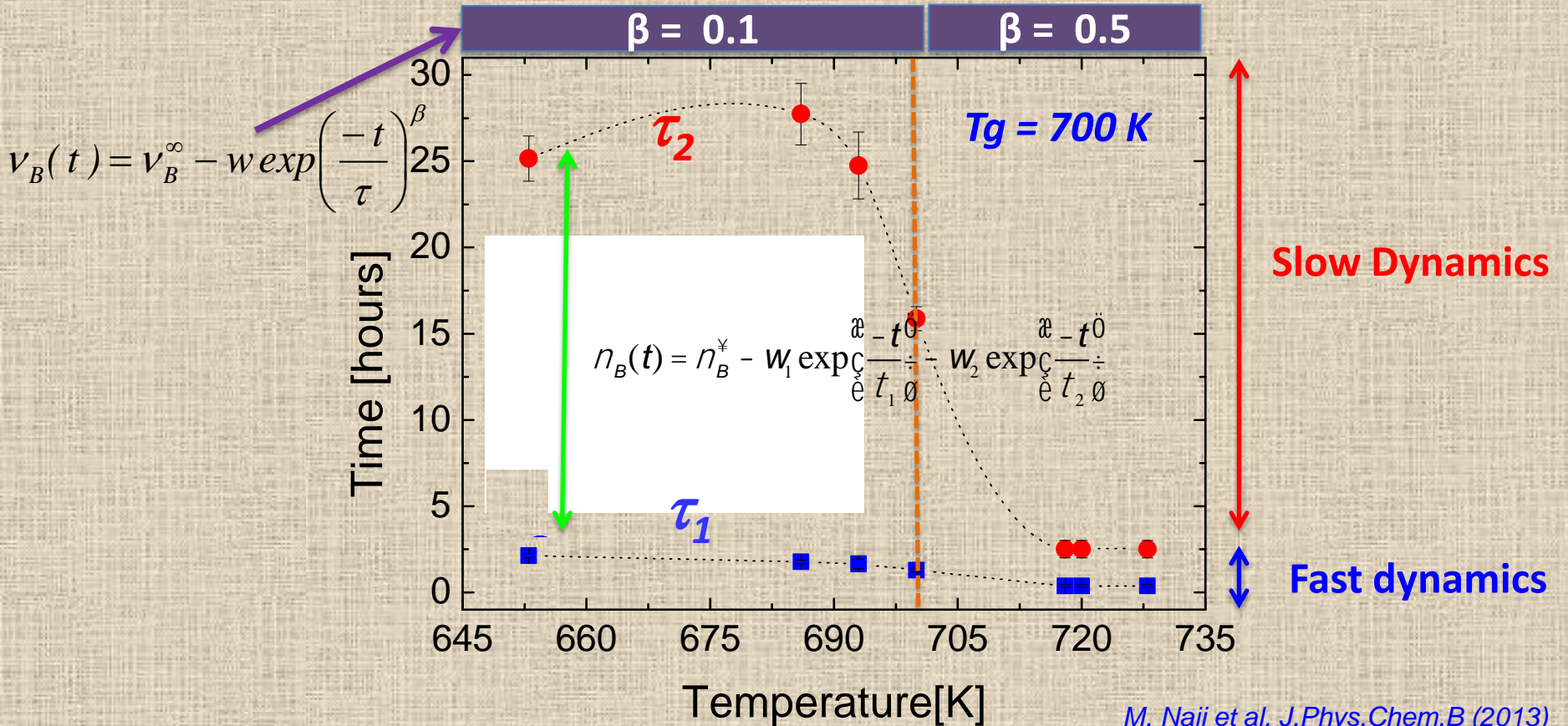
→ bi-exponential model

$$n_B(t) = n_B^\infty - w_1 \exp\left(-\frac{t}{t_1}\right) - w_2 \exp\left(-\frac{t}{t_2}\right)$$

→ Stretched exponential

$$n_B(t) = n_B^\infty - w \exp\left(-\frac{t}{t_0}\right)^b \quad \text{with } 0 < b \leq 1$$

Evidence of heterogeneous dynamics



M. Naji et al. *J.Phys.Chem.B* (2013)
 M.Naji et al. *Physics Procedia* (2013)

→ $T < T_g$: two relaxations τ_1 & τ_2
 one order of magnitude, or
 small β strong heterogeneity

→ $T > T_g$: weak heterogeneity

→ Evidence of an heterogeneous dynamics at long distance

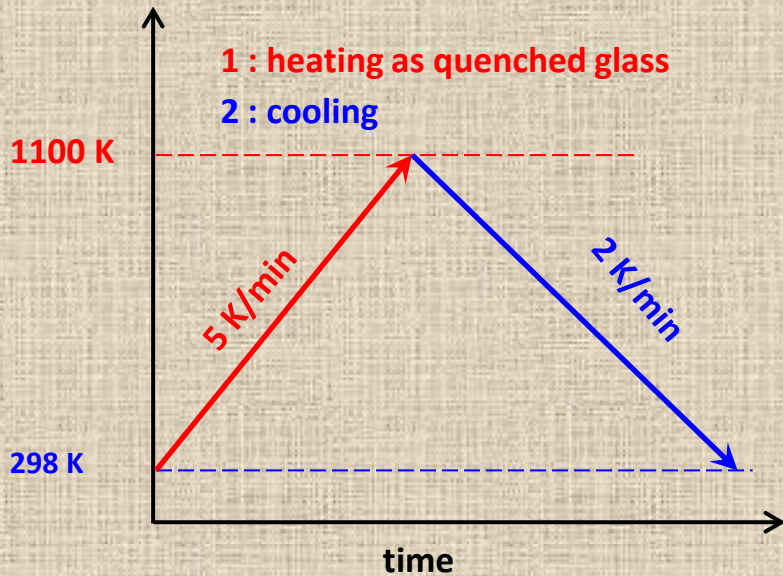
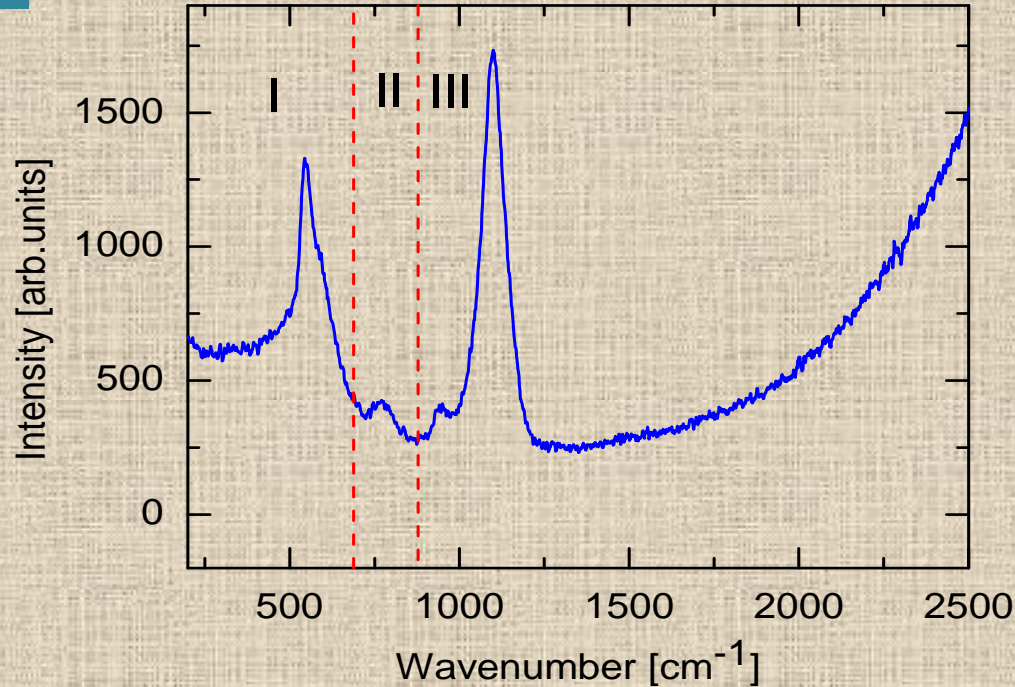
structurale relaxation at short distance: **Raman**

Raman modes of the Raman spectrum

Region I: 3, 4, 5 et 6 tetrahedra rings

Region II: Si-O-Si interterahedral bonds

Region III: Si-NBO/BO in Q^n species

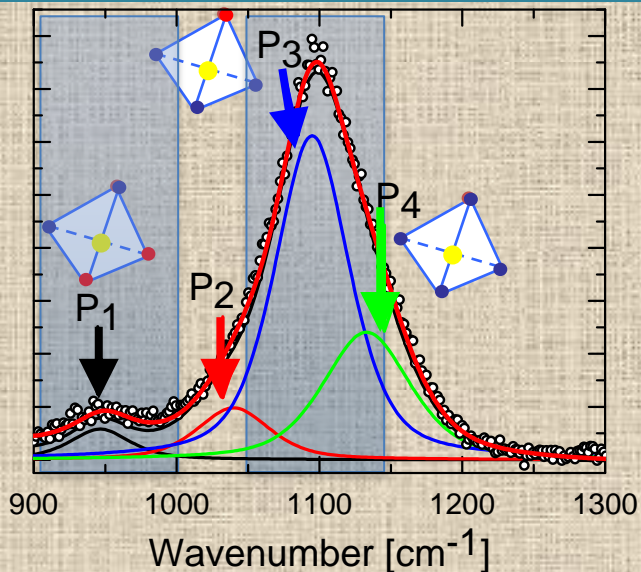


Experimental process : in situ heating and cooling

short range by Raman vs temperature

Analyse in individual compounds

4 gaussian bands

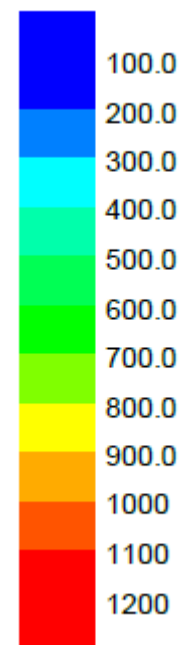
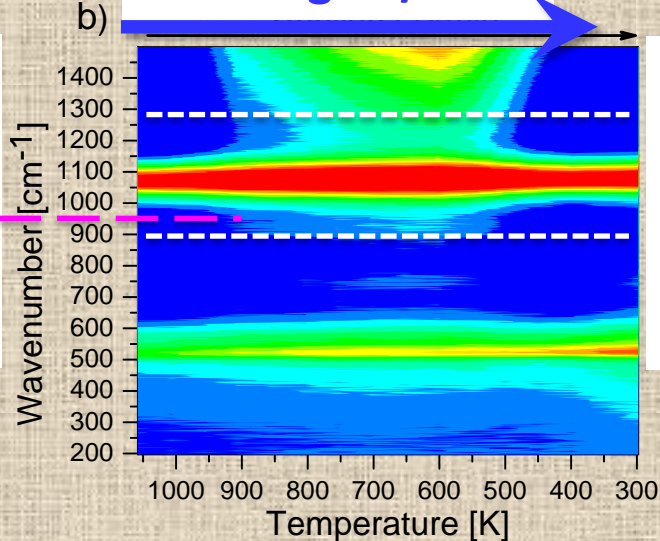
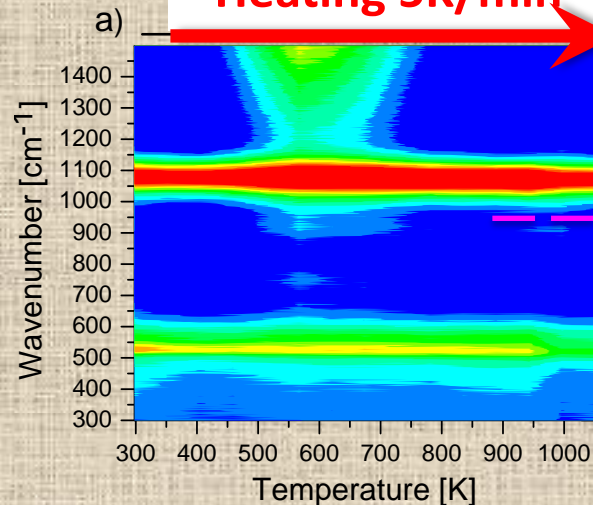


- P1 Mode → stretching Si-NBO in Q² species
- P2 Mode → stretching Si-BO
- P3 Mode → stretching Si-NBO in Q³ species
- P4 Mode → stretching Si-NBO in Q⁴ species

*D. De Sousa Meneses Vibrational Spectroscopy, 65, 50-57 2013.
W.J. Malfait, J. Raman Spec. 2009*

Heating 5K/min

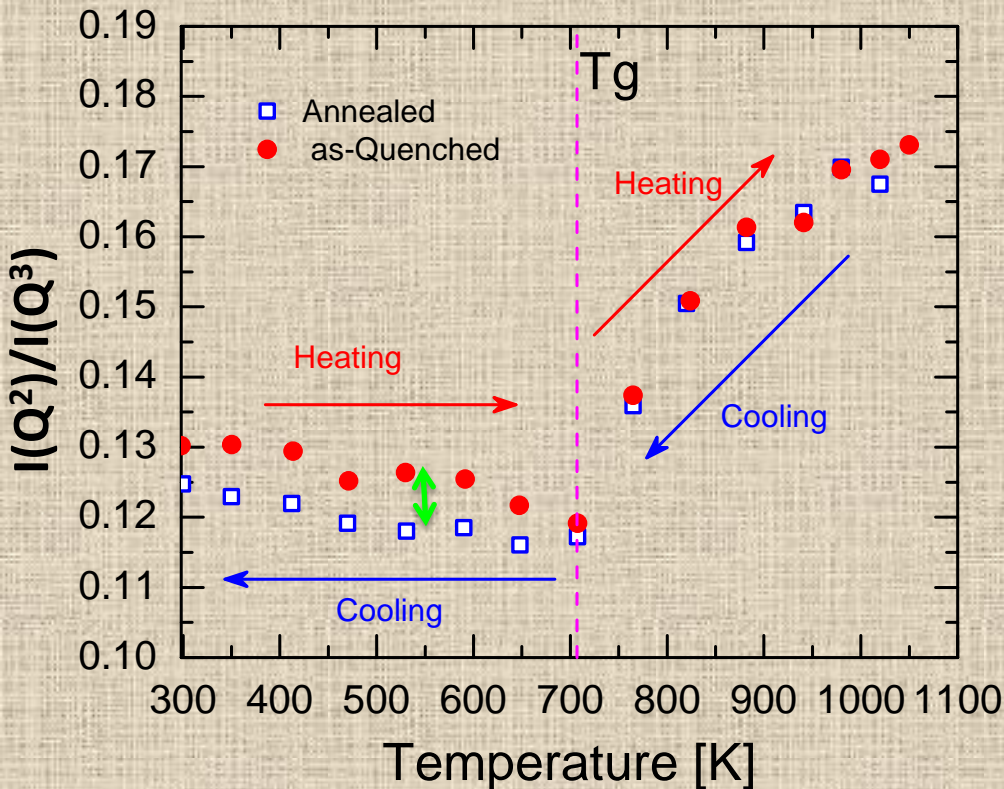
Cooling 2K/min



✓ quasi-Reversible

Evidence of relaxation at short range

Variations of Q^2 line relative intensity with the temperature



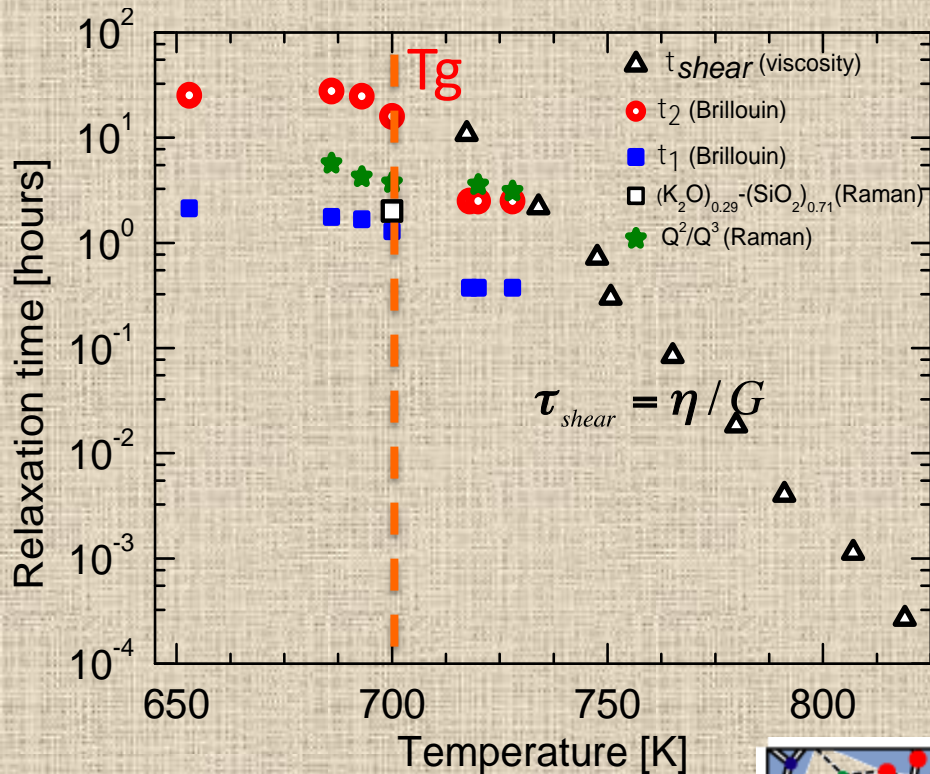
- ~~Reduction of number of Q^2 (Si-O) species by relaxation ?~~
- Variation of the Raman cross section (Environment change) ?

The well known NMR measurements
exclude the first hypothesis

the intensités of Q^2/Q^3 ratio → good probe for structural relaxation

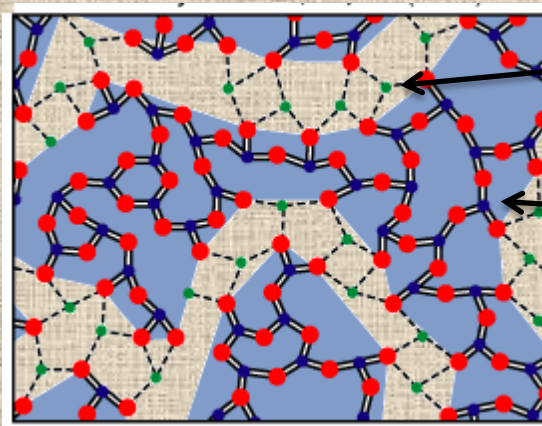
Discussion

Comparison of several relaxation dynamics
(Brillouin, Raman, viscosité)



Temps de relaxation Raman (Q^2/Q^3)
relaxation time : close from the **fast**
Brillouin τ_2

The Brillouin **slow relaxation** time τ_1
is consistent with shear relaxation
time deduced from the viscosity :
Si—O—Si

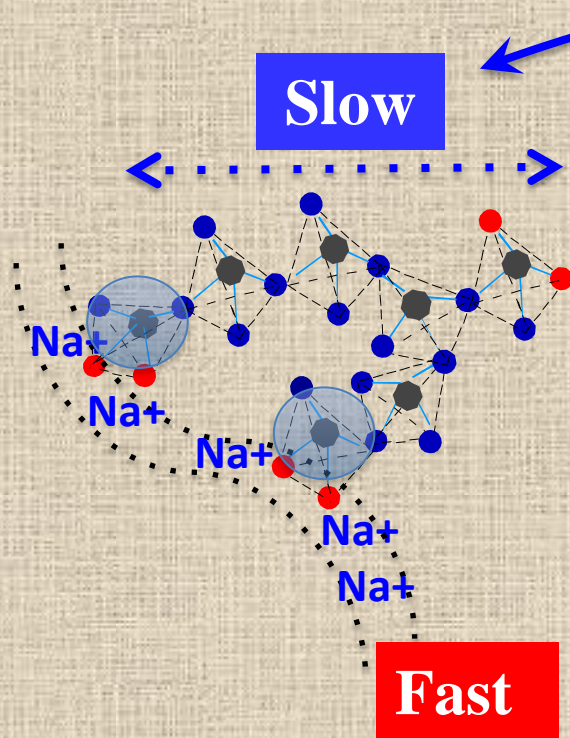


Na^+
ions

$Q^{n<4}$
species

Conclusion

Relaxation scenario at $T < T_g$ and heterogeneous dynamics



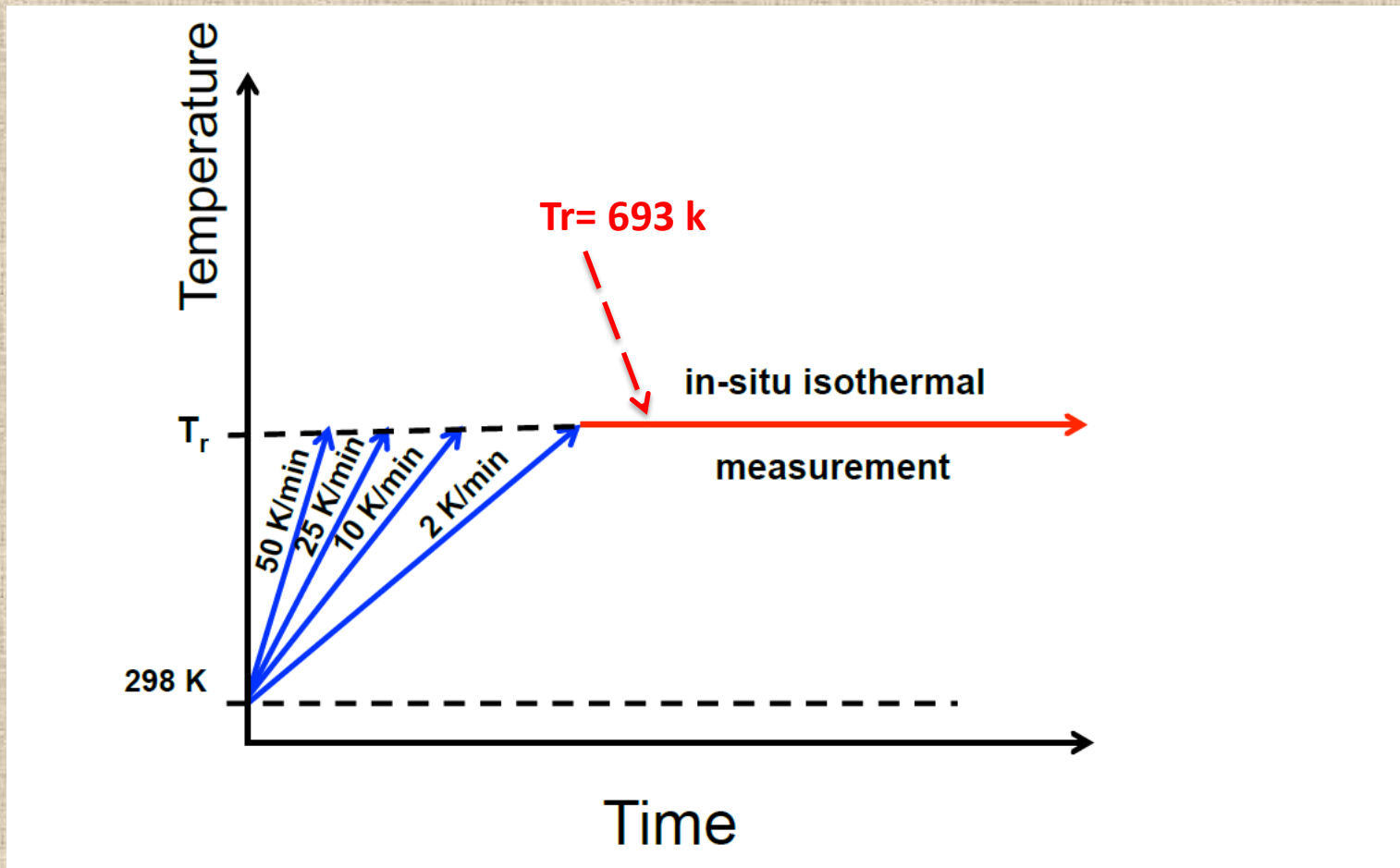
The **Brillouin slow relaxation** time τ_1 is consistent with shear relaxation time deduced from the **viscosity** :
Si—O--Si

Temps de relaxation **Raman** (Q^2/Q^3) relaxation time : close from the **fast Brillouin** τ_2

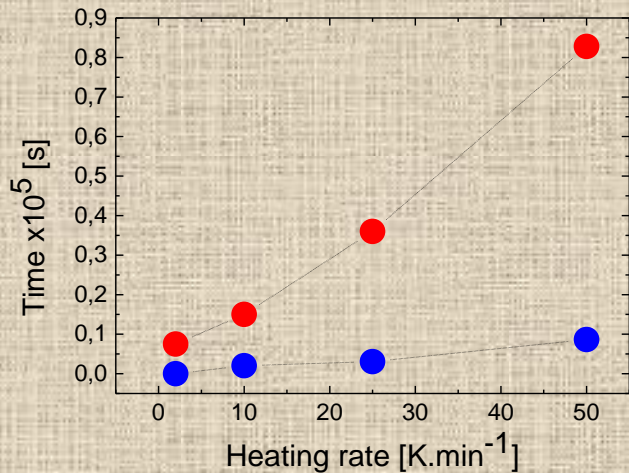
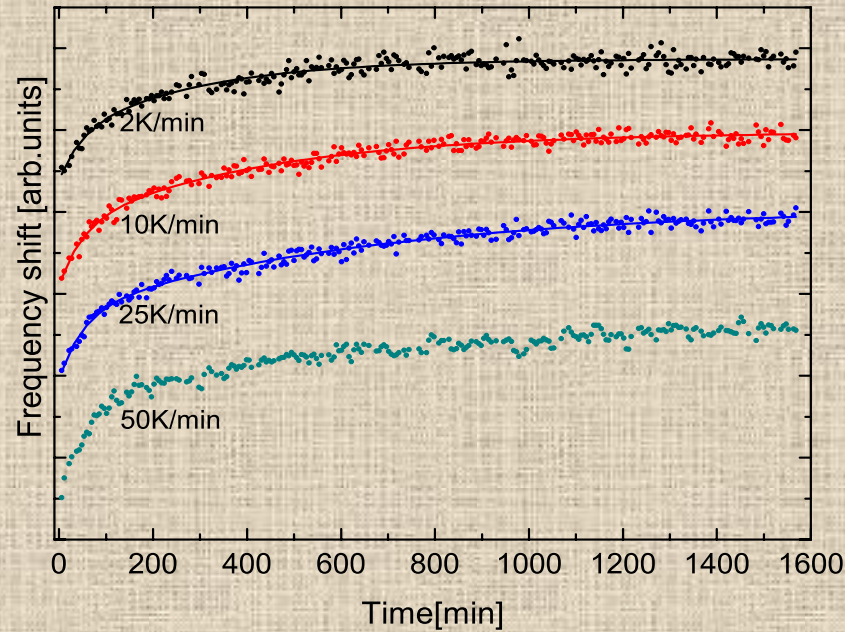
Effet de la vitesse de montée en température

Thinks are they so simple?

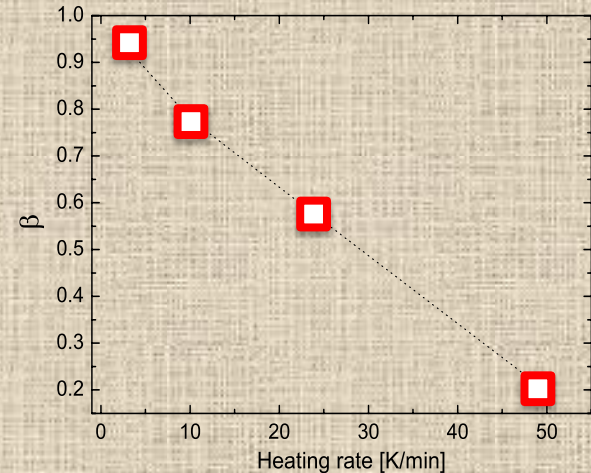
Effect of heating rate



Effect of heating rate



$$n_B(t) = n_B^\infty - w_1 \exp\left(-\frac{t}{t_1}\right) - w_2 \exp\left(-\frac{t}{t_2}\right)$$

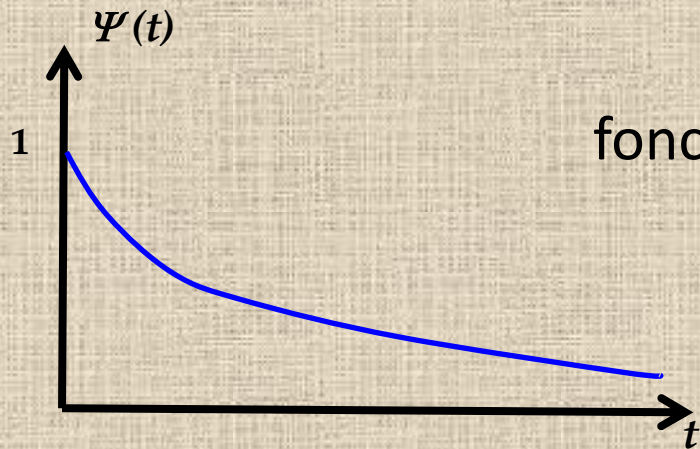


$$v_B(t) = v_B^\infty - w \exp\left(-\frac{t}{\tau}\right)^\beta$$

Idea of time relaxation distribution function

Modélisation using fractional Brownian
dynamics

G. Kneller, J; Chem. Phys. (2010)



fonction de relaxation = superposition
d'exponentielles

$$\Psi(t) = \int_0^{\infty} d\lambda p(\lambda) e^{-\lambda t}$$

$p(\lambda)$ représente ici le spectre de taux de relaxation

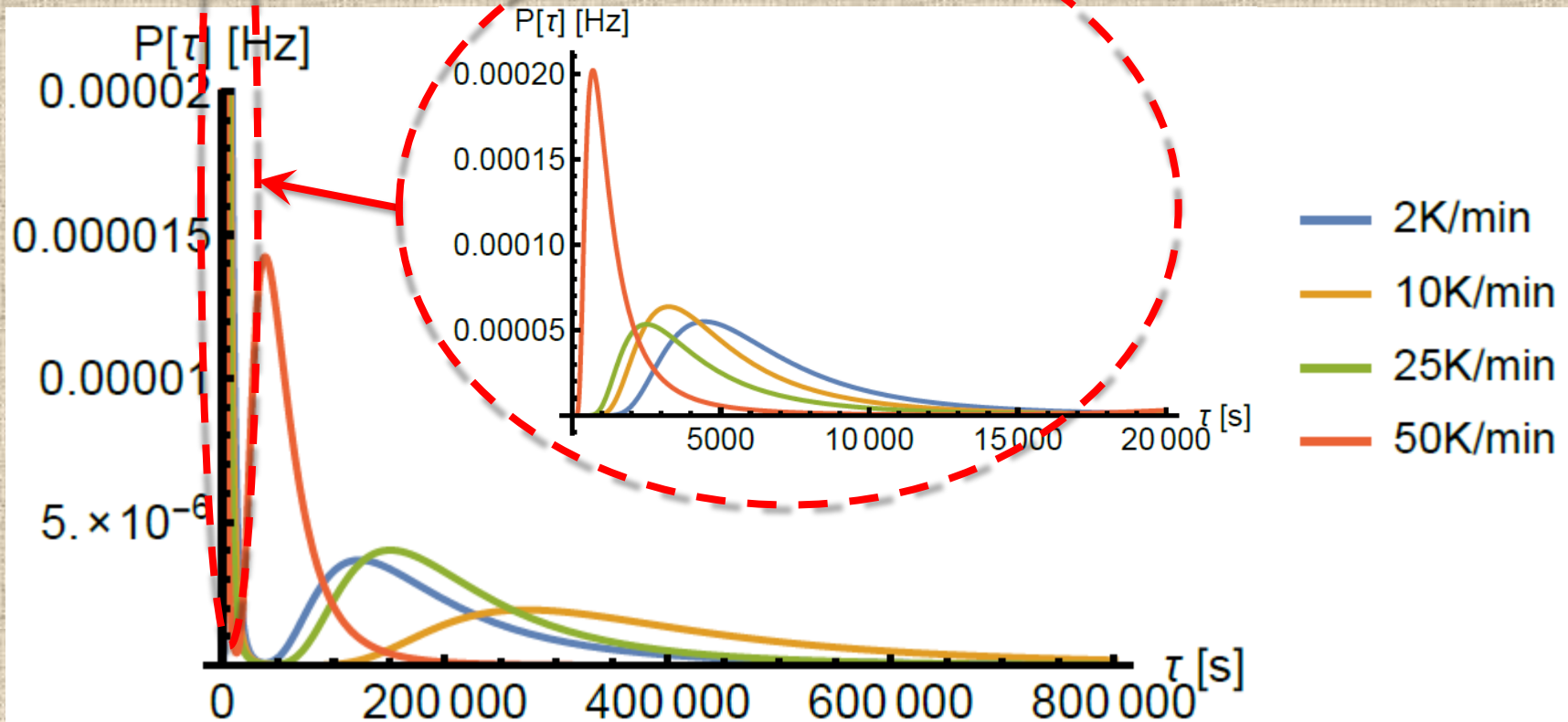
Effect of heating rate

Idea of time relaxation distribution function

Modelisation using fractional Brownian dynamics

G. Kneller, J; Chem. Phys. (2010)

Relaxation spectra



Détails techniques

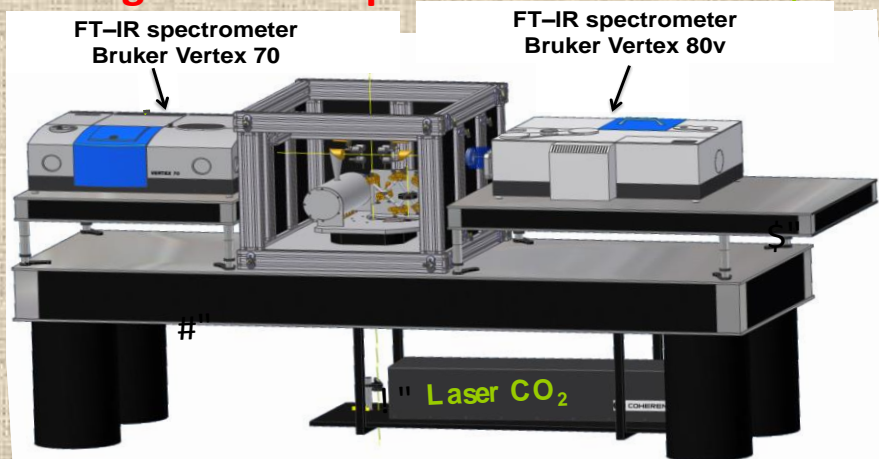
Dispositif expérimental : 2 spectromètres

développé au CEMHTI

spectromètre FT-IR, Bruker Vertex 80v

$\sigma = 400 - 1600 \text{ cm}^{-1}$

Chauffage avec une platine résistive $T \sim 1200 \text{ K}$



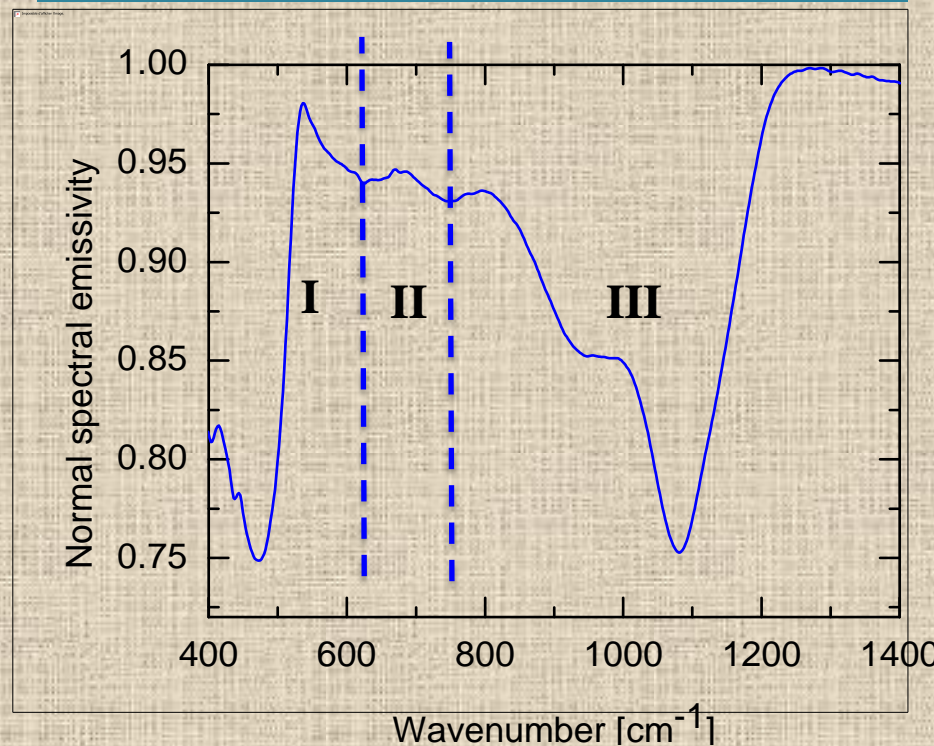
Calcul d'emissivité

Luminance du verre et celle du corps noir

$$E = \frac{TF(I_S - I_{RT})}{TF(I_{BB} - I_{RT})} \frac{P_{BB} - P_{RT}}{P_S - P_{RT}} E_{BB}$$

FT : Fourier transform ; I : Interferogram ; P: Planck's law ; BB : Black body ; S: Sample ; RT : Room Temperature

Spectre d'emissivité du verre



- région I : **fléxion** des liaisons O—Si—O
- région II : **vibrations** des liaisons Si—O—Si
- région III: **vibration** des liaison Si—BO/NBO dans les entités Q^n

Région opaque : Lois de Kirchhoff et Fresnel

$$E(\omega) = 1 - \left| \frac{\sqrt{\epsilon(\omega)} - 1}{\sqrt{\epsilon(\omega)} + 1} \right|^2$$

avec :

$$\epsilon(\omega) = \epsilon'(\omega) + i\epsilon''(\omega)$$

fonction diélectrique

Attribution des modes

ν_1 O-Si-O déformation

ν_2 Si-O-Si étirement, ν_6

ν_3 Si-NBO étirement dans Q^2

ν_4 Si-NBO étirement dans Q^3

ν_5 Si-BO étirement dans Q^4

ν_7 Si-BO contribution des Q^2, Q^3, Q^4
au désordre dynamique

Logiciel Focus



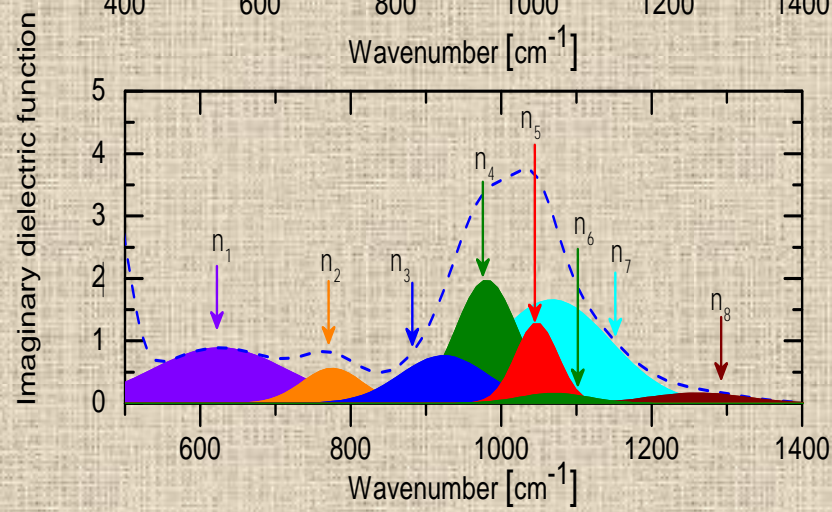
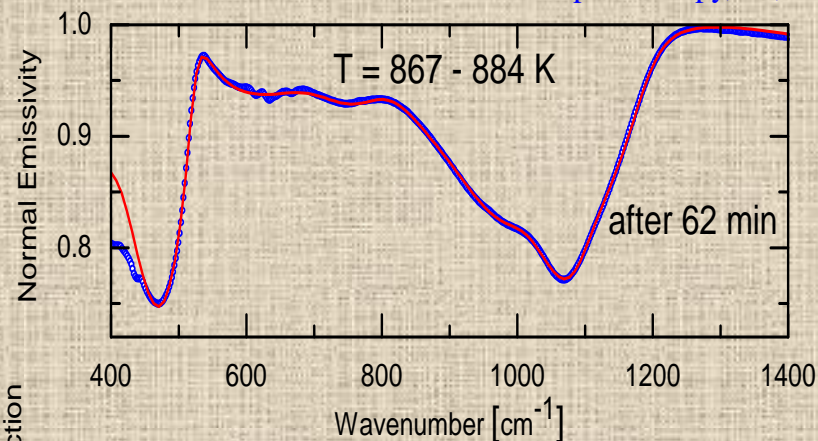
Modèle utilisant un profil d'absorption gaussien

$$\epsilon(\omega) = \epsilon_\infty + \sum_j (g_j^{kkg}(\omega) + ig_j(\omega))$$

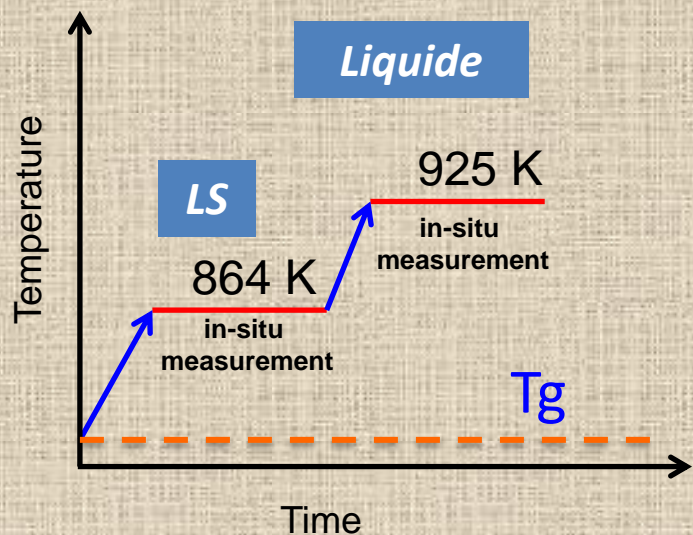
contributions électroniques

gaussienne causale

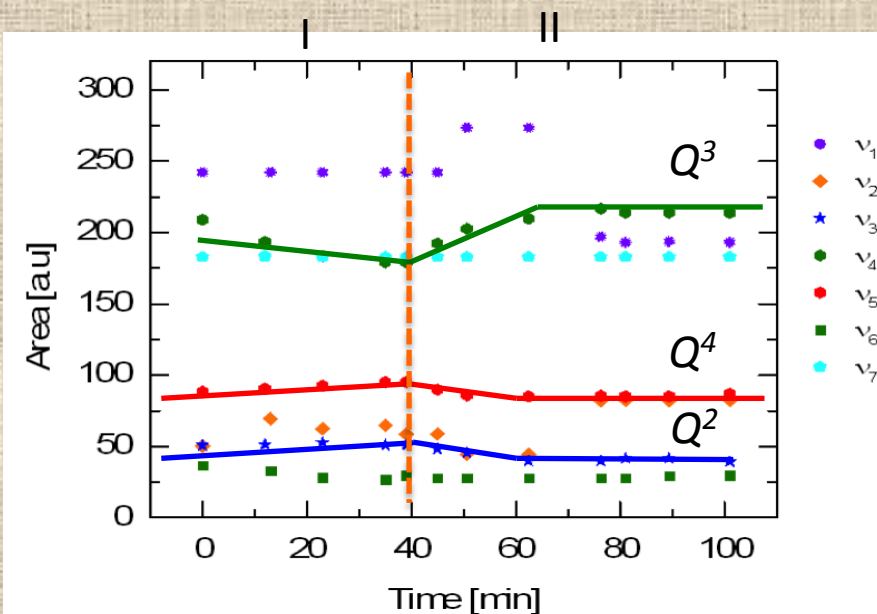
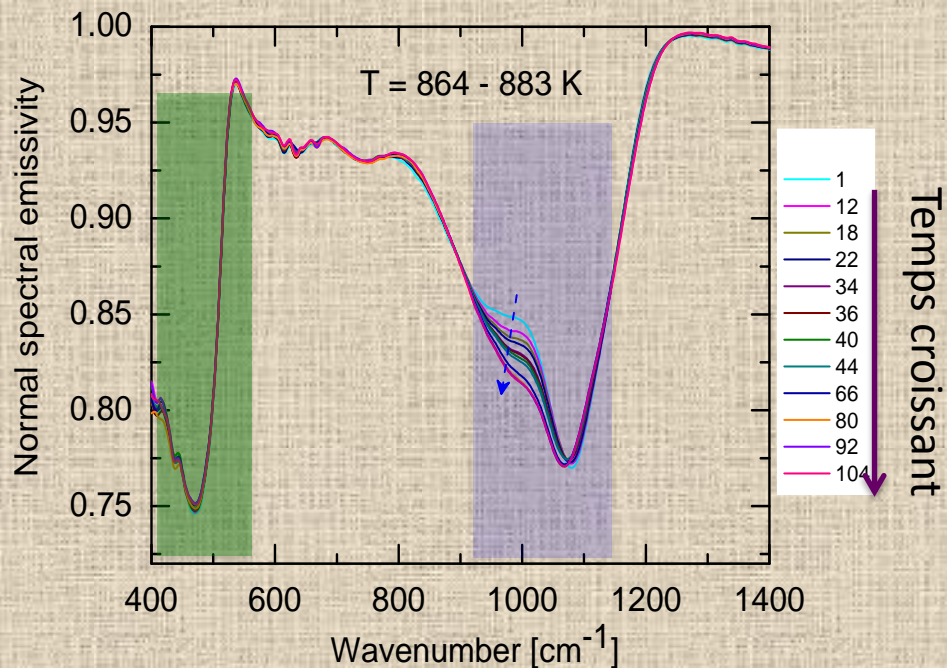
D. De Sousa Meneses Vibrational Spectroscopy, 65, 50-57 2013.



Protocol expérimental



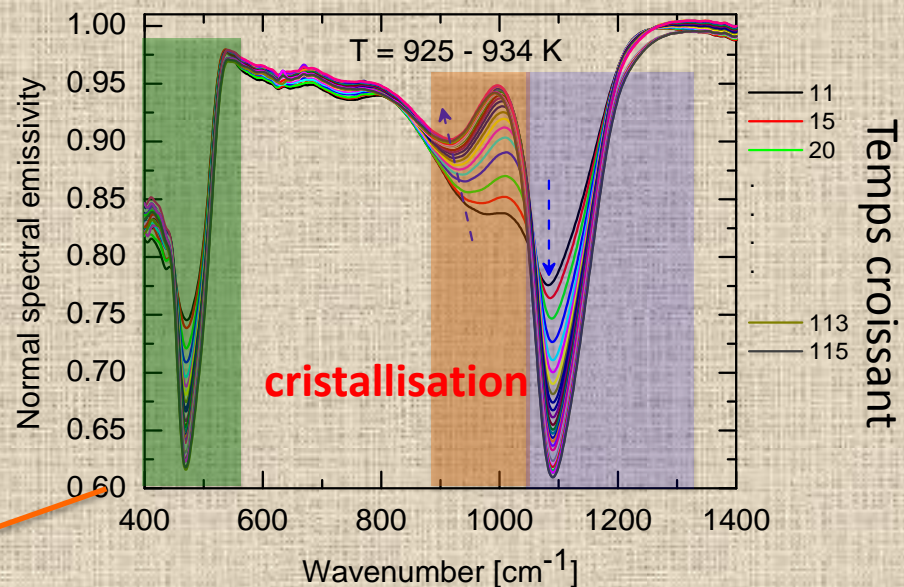
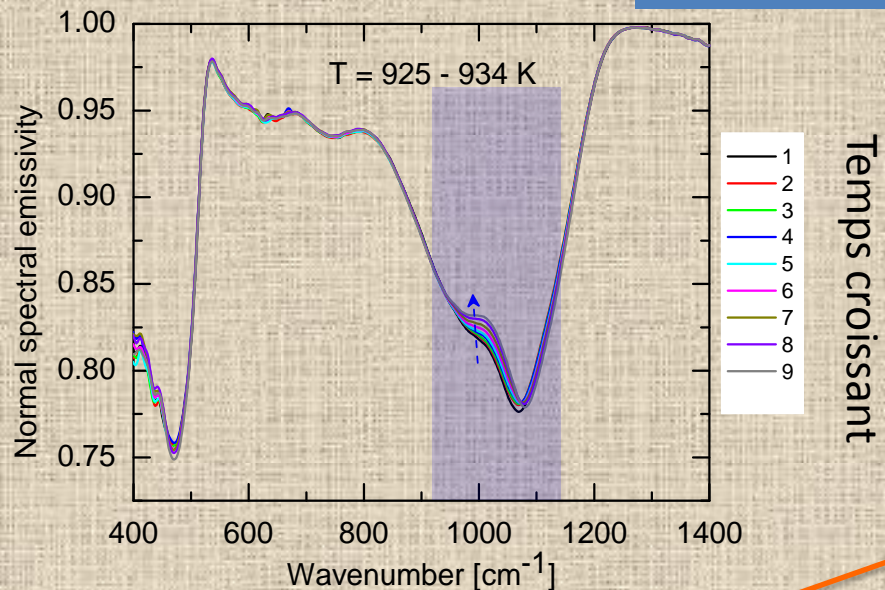
LS



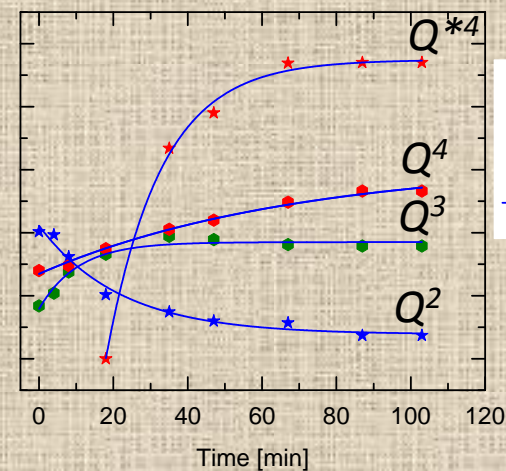
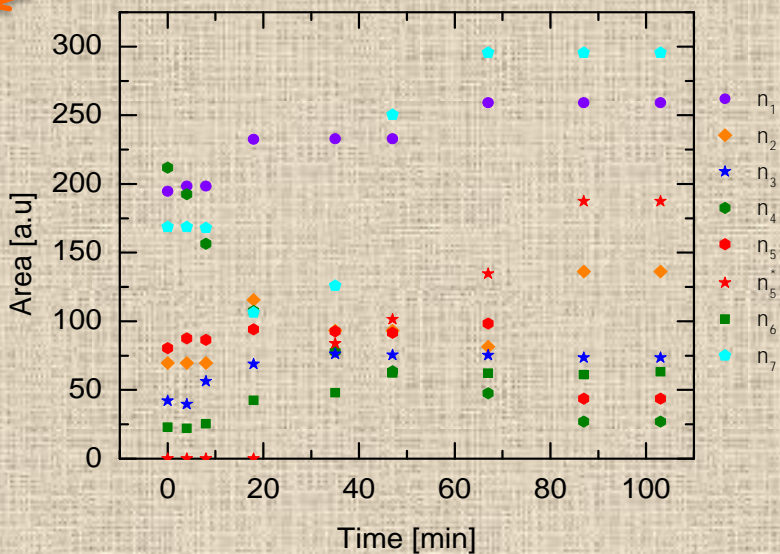
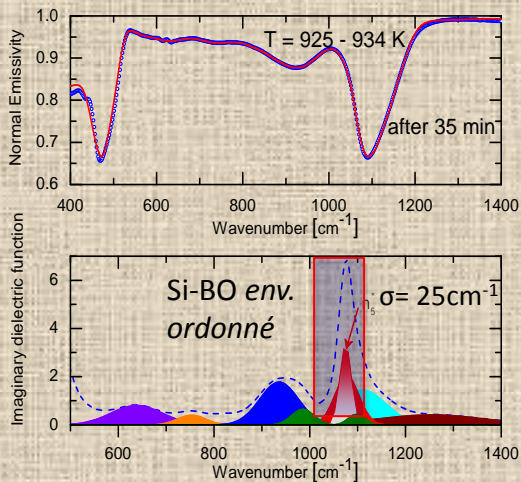
- Le phénomène de relaxation s'amorce.
- Augmentation de l'aire Q^3 et diminutions des aires Q^2 , Q^4

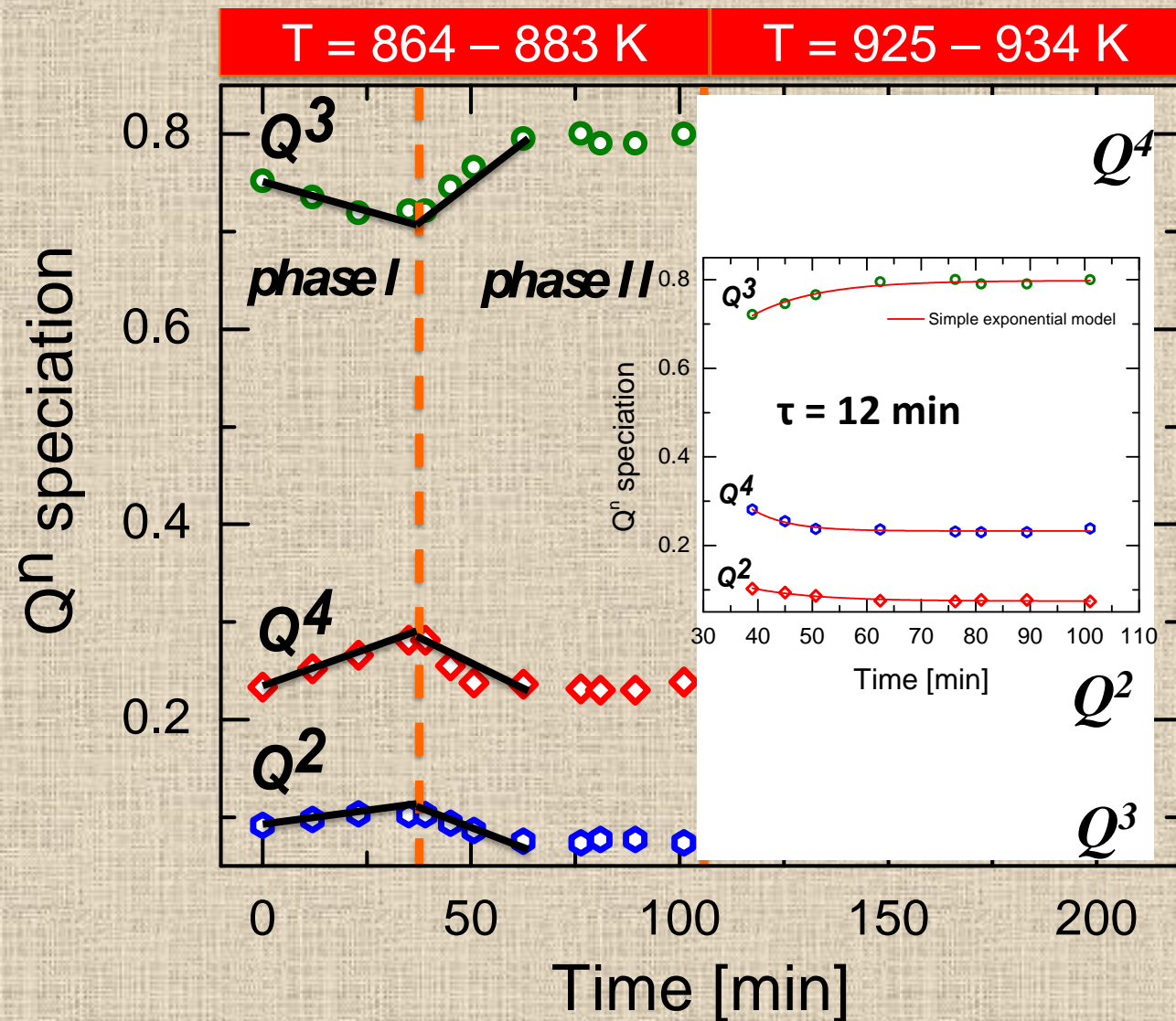
1. Mise en place d'une réorganisation qu'on voit pas par Infrarouge.
2. Puis relaxation à courte distance, avec changement des populations Q^n .

Liquide



Ajout d'un mode supplémentaire:
 Q^4 (SiO_2 -quartz)





- ✓ Augmentation des entités Q²
- ✓ Verre continue à évoluer, état plus table.
- ✓ Augmentation des entités Q⁴.
- ✓ Migration des Na⁺ pour compenser la charge.
- ✓ Augmentation des espèces Q⁴, appaition du mode $2Q_3 \rightleftharpoons Q_4 + Q_2$
- ✓ Consommation de 2Q³.
- ✓ Le système atteint un minimum, montre la formation d'une phase cristalline riche de SiO₂- quartz.

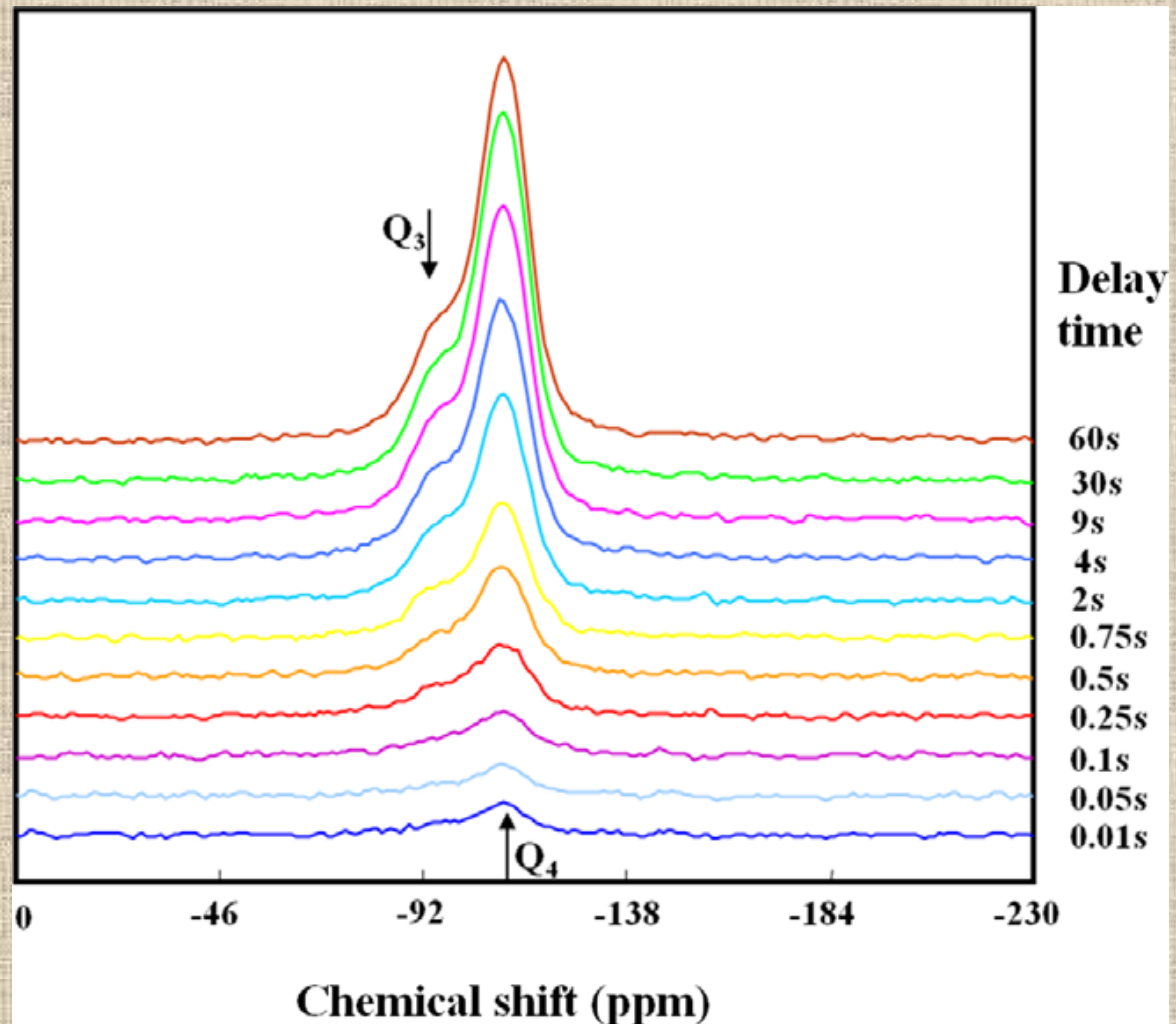
➔ Cristallisation et réaction lente du système au début, mise en place d'une organisation à longue distance, puis une relaxation à courte échelle.

Etude par RMN de la distribution spatiale des ions Na^+ dans les verres $(\text{SiO}_2)_{1-x}(\text{Na}_2\text{O})_x$

distribution spatiale
des atomes porteurs
de moments
magnétiques (ici ^{29}Si)
 \Rightarrow relation masse-
distance

$$m(r) \sim r^D$$

^{29}Si Chemical shift in
9Na₂O–91SiO₂ glass (1000
ppm Gd₂O₃).



$M(t) = t^\alpha$ relaxation nucléaire de ^{29}Si

$$M(t) = c \int_{r_m}^{r_M} [1 - \exp(-At / r^6)] \mu_0(r) dr$$

$$M(t) = c M_0 [r = (At)^{1/6}]$$

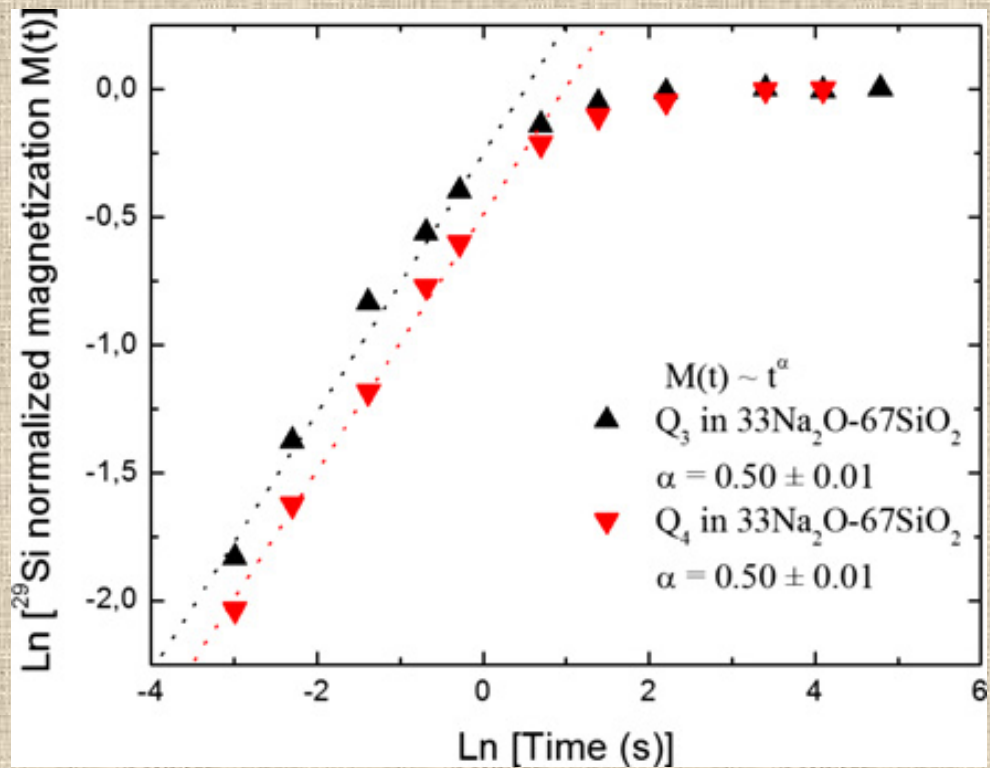
$$M \propto r^D \propto t^\alpha \propto (At)^{D/6}$$

$$\Rightarrow \alpha = D/6$$

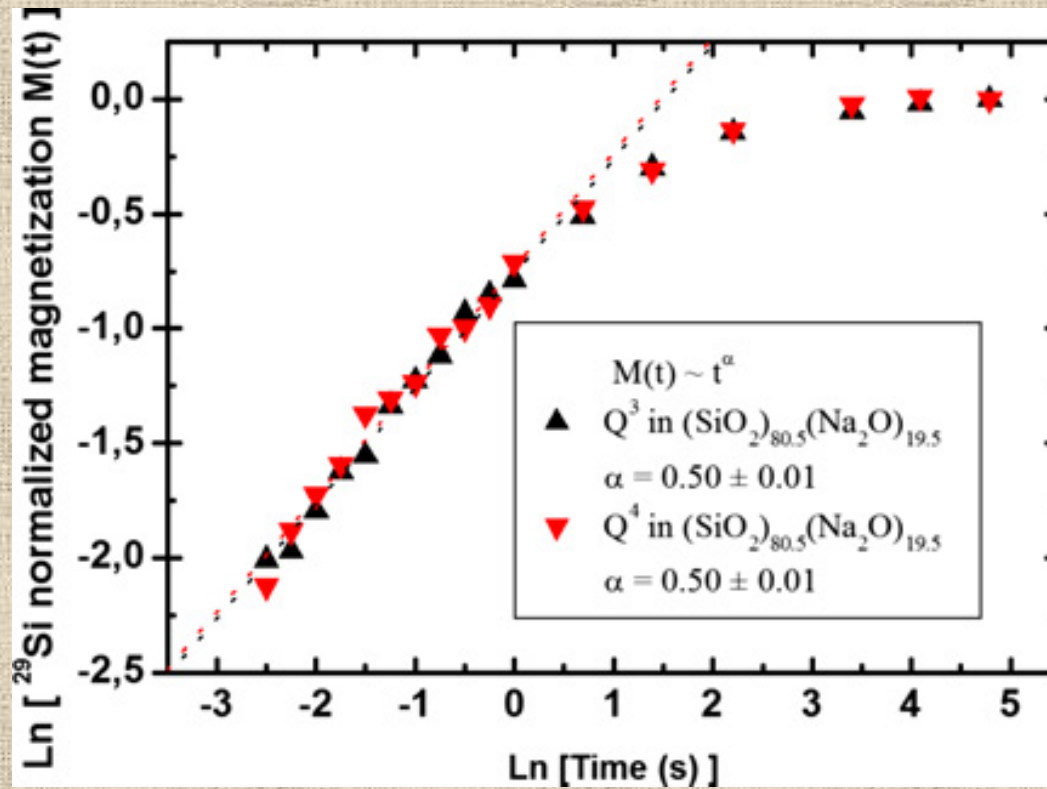
$$(\text{SiO}_2)_{0.91}(\text{Na}_2\text{O})_{0.09} \Rightarrow D = 2.46$$

$$(\text{SiO}_2)_{0.795}(\text{Na}_2\text{O})_{0.195} \Rightarrow D \approx 3$$

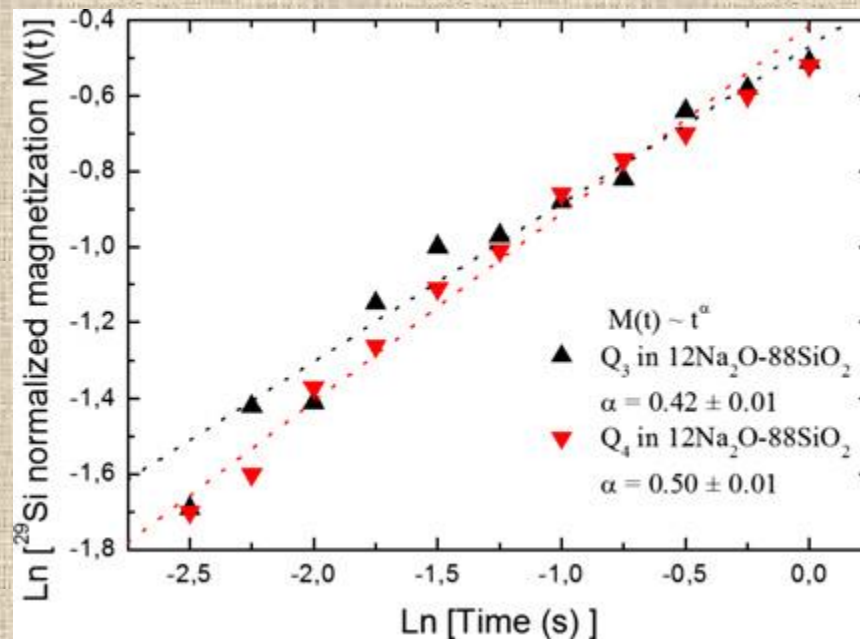
$$(\text{SiO}_2)_{0.68}(\text{Na}_2\text{O})_{0.32} \Rightarrow D \approx 3$$



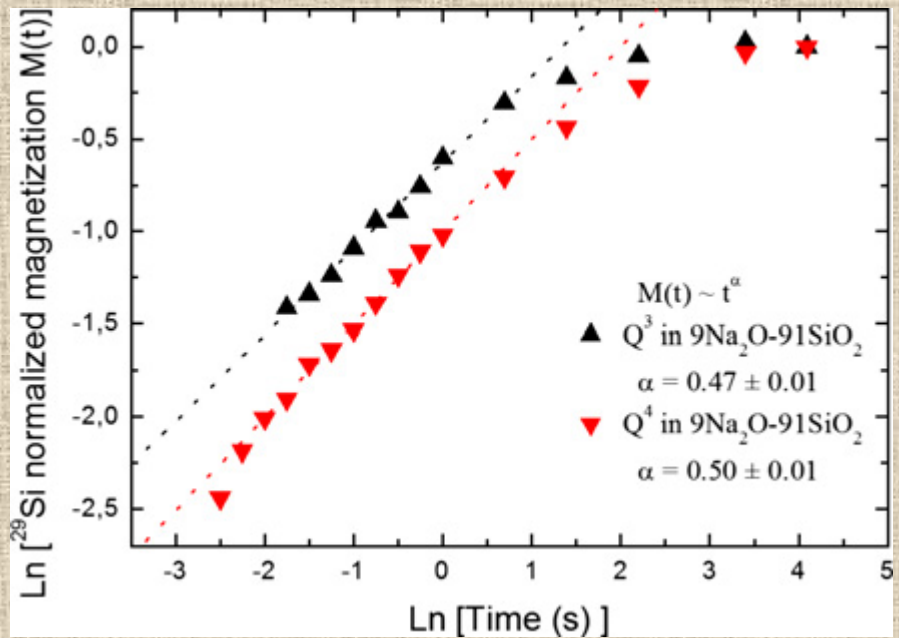
Logarithm of ^{29}Si normalized magnetization as a function of logarithm time delay for $33\text{Na}_2\text{O}-67\text{SiO}_2$ glass (e).



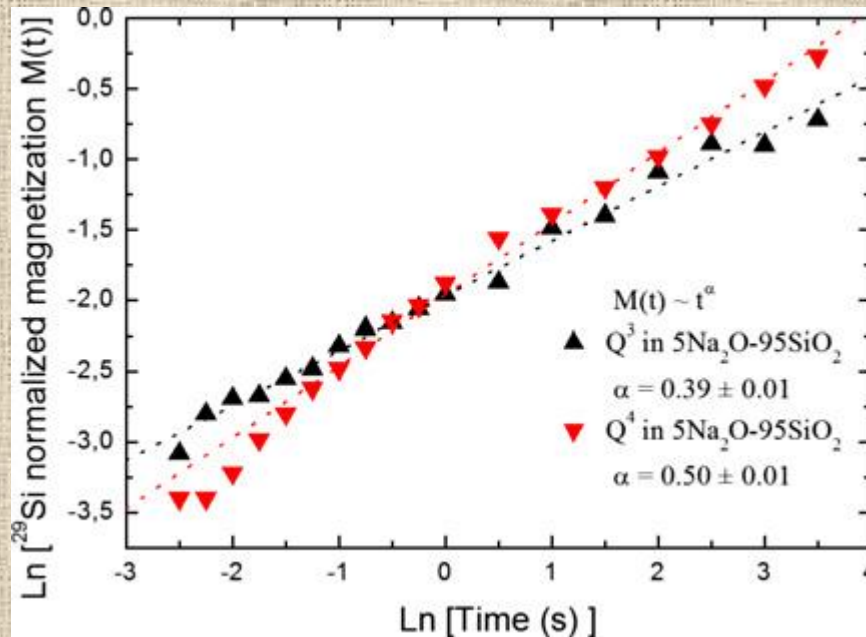
Logarithm of ²⁹Si normalized magnetization as a function of logarithm time delay for 19.5Na₂O–80.5SiO₂ glass



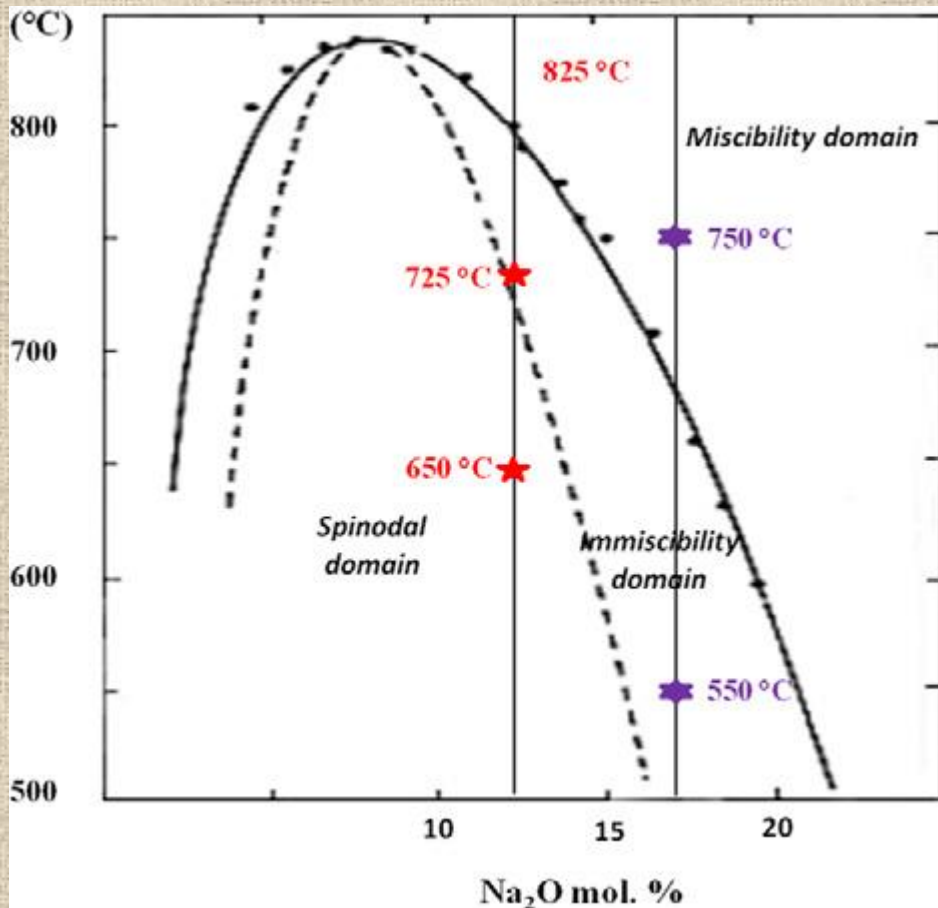
Logarithm of ²⁹Si normalized magnetization as a function of logarithm time delay for 12Na₂O– 88SiO₂ glass



Logarithm of ^{29}Si normalized magnetization as a function of logarithm time delay for $9Na_2O-91SiO_2$ glass

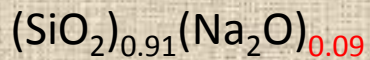


Logarithm of ²⁹Si normalized magnetization as a function of logarithm time delay for 5Na₂O–95SiO₂ glass

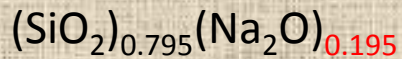


$$M \propto r^D \propto t^\alpha \propto (At)^{D/6}$$

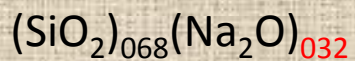
$$\Rightarrow \alpha = D/6$$



$$(\text{SiO}_2)_{0.91}(\text{Na}_2\text{O})_{0.09} \Rightarrow D = 2.46$$

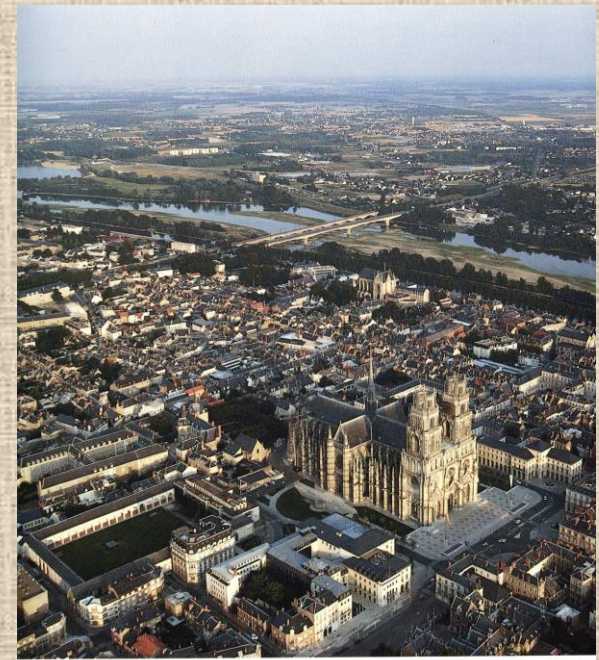


$$(\text{SiO}_2)_{0.795}(\text{Na}_2\text{O})_{0.195} \Rightarrow D \approx 3$$



$$(\text{SiO}_2)_{0.68}(\text{Na}_2\text{O})_{0.32} \Rightarrow D \approx 3$$

Thank you for
your attention



Orléans city
Joan of Arc City

along
Loire river

“Loire valley”
also named
“Kings valley”

University
Since 1306